LEARNING RESOURCE MATERIAL COURSE CODE- Th 2 HYDRAULICS ENGINEERING

DEPARTMENT

OF

CIVIL ENGINEERING

GOVERNMENT POLYTECHNIC KENDRAPARA



PREPARED BY

ANITA PRADHAN LECTURER IN CIVIL ENGINEERING

COURSE OBJECTIVES

On completion of the course students will be able to -

1. Define common fluid properties and interpret results from pressure measuring instruments.

2. Realize the science behind fluid flow and compute fluid flow characteristics through notches, weirs, channels and pipes.

3. Realize the working principle of hydraulic pumps and evaluate their performance in general cases.

4. Comprehend the need of irrigation

5. Determine cause and effect of water logging

6. Comprehend the purpose of irrigation system components and elaborate on these

Chapter	Name of topics	PAGE NO
1	Hydrostatics	3-13
2	Kinematics Of Fluid Flow	14-45
3	Pumps	46-55
10	Dams	56-73

CONTENTS

Chapter-I

HYDROSTATICS

Hydrostatic is that branch of science which relating to fluids at rest or to the pressures they exert or transmit **Hydrostatic Pressure**.

Fluid:-

Fluid is a substance that continuously deforms (flows) under an applied shear stress. Fluids are a subset of the phase of matter and include liquids, gases, plasmas and, to some extent, plastic solids. Fluids can be defined as substances which have zero shear modulus or in simpler terms a fluid is a substance which cannot resist any shear force applied to it.

- Fluid is a substance which is capable of flowing
- Conform the shape of the containing vessel
- ✤ Deform continuously under application of small shear force

PROPERTIES OF FLUID:-

Density:-

The density of a fluid, is generally designated by the Greek symbol $\rho(rho)$ is defined as the mass of the fluid over a unit volume of the fluid at standard temperature and pressure. It is expressed in the SI system as kg/m³.

$$\rho = \lim \frac{\Delta m}{\Delta V} = \frac{dm}{dV}$$

If the fluid is assumed to be uniformly dense the formula may be simplified as:

$$\rho = \frac{m}{V}$$

Example: - setting of fine particles at the bottom of the container.

Specific Weight:-

The specific weight of a fluid is designated by the Greek symbol γ (gamma), and is generally defined as the weight per unit volume of the fluid at standard temperature and pressure. In SI systems the units is N/m³.

 $\lambda = \rho * g$

 $g = \text{local acceleration of gravity and } \rho = \text{density}$ *Note:* It is customary to use: $g = 32.174 \text{ ft/s}^2 = 9.81 \text{ m/s}^2$ $\rho = 1000 \text{ kg/m}^3$

Relative Density (Specific Gravity):-

The relative density of any fluid is defined as the ratio of the density of that fluid to the density of the standard fluid. For liquids we take water as a standard fluid with density ρ =1000 kg/m³. For gases we take air or O₂ as a standard fluid with density, ρ =1.293 kg/m³.

Specific volume:-

Specific volume is defined as the volume per unit mass. It is just reciprocal of mass density. It is expressed in m^3/kg .

Viscosity:-

Viscosity (represented by μ , Greek letter mu) is a material property, unique to fluids, that measures the fluid's resistance to flow. Though a property of the fluid, its effect is understood only when the fluid is in motion. When different elements move with different velocities, each element tries to drag its neighboring elements along with it. Thus, shear stress occurs between fluid elements of different velocities.

Viscosity is the property of liquid which destroyed the relative motion between the layers of fluid.

- \clubsuit It is the internal friction which causes resistance to flow.
- Viscosity is the property which control the rate of flow of liquid

Viscosity is due to two factors-

- a) Cohesion between the liquid molecules.
- b) Transfer of momentum between the molecules.

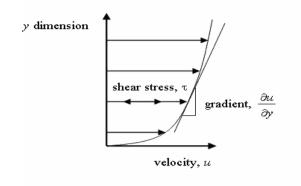


Fig. 1.1

The relationship between the shear stress and the velocity field was that the shear stresses are directly proportional to the velocity gradient. The constant of proportionality is called the coefficient of dynamic viscosity.

$$\tau = \mu \frac{\partial u}{\partial y}$$

UNIT OF VISCOSITY

- In mks system unit of viscosity is kgf-sec/m²
- ✤ In cgs system unit of viscosity is dyne-sec/cm²
- ✤ In S.I system unit of viscosity is Newton-sec/m²

Kinematic viscosity:-

Another coefficient, known as the kinematic viscosity (ν , Greek nu) is defined as the ratio of dynamic viscosity and density.

I.et, $\upsilon = \mu / \rho$ = viscosity/density

In mks & S.I system unit of kinematic viscosity is meter²/sec

In cgs system unit of kinematic viscosity is stoke.

SURFACE TENSION:-

Surface tension is defined as the tensile force acting on the surface of a liquid in contact with a gas or on the surface between two immiscible liquids such that the contact surface behaves like a membrane under tension. The magnitude of this force per unit length of the free surface will have the same value as the surface energy per unit area. It is denoted by Greek letter sigma(σ). In MKS units, it is expressed as kgf/m while in SI unit is N/m.

It is also defined as force per unit length, or of energy per unit area. The two are equivalent but when referring to energy per unit of area, people use the term surface energy—which is a more general term in the sense that it applies also to solids and not just liquids.

Capillarity:-

Capillarity is defined as a phenomenon of rise or fall of a liquid surface in a small tube relative to the adjacent general level of liquid when the tube is held vertically in the liquid. The rise of liquid surface is known as capillary rise while the fall of the liquid surface is known as capillary depression. It is expressed in terms of cm or mm of liquid. Its value depends upon the specific weight of the liquid, diameter of the tube and surface tension of the liquid.

Pressure and its measurement:-

INTENSITY OF PRESSURE:-

Intensity of pressure is defined as normal force exerted by fluid at any point per unit area. It is also called specific pressure or hydrostatic pressure

P=df/da

If intensity of pressure is uniform over an area "A" then pressure force exerted by fluid equal to

Mathematically F=PA

If intensity of pressure is not uniform or vary point to point then pressure force exerted by fluid equal to integration of P*A

Mathematically $F=\int PA$

- ✤ Unit of pressure
 - $1N/m^2 = 1$ Pascal
 - 1KN/m²= 1 kilo Pascal
 - Kilo Pascal= 1kpa = 10^3 Pascal
 - 1 bar = 10^5 Pascal = 10^5 N/m²

Pascal's law:-

It states that the pressure or intensity of pressure at a point in a static fluid is equal in all direction.

Atmospheric Pressure:-

7

The atmospheric air exerts a normal pressure upon all surface with which it is in contact and it is called atmospheric pressure. It is also called parametric pressure.

Atmospheric pressure at the sea level is called standard atmospheric pressure.

S.A.P = 101.3 KN/m² = 101.3 kpa = 10.3 m of H₂O

= 760 mm of Hg

=10.3 (milli bar)

Gauge pressure:-

It is the pressure which measure with help of pressure measuring device in which atmospheric pressure taken as datum.

The atmospheric pressure on scale is marked as zero.

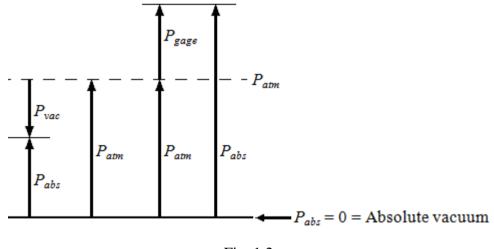
Absolute pressure:-

Any pressure measure above absolute zero pressure is called absolute pressure.

Vacuum pressure:-

Vacuum pressure is defined as the pressure below the atmospheric pressure.

RELATIONSHIP BETWEEN ABSOLUTE PRESSURE, GAUGE PRESSURE, VACUUM PRESSURE:-





Equations

$P_{\text{gage}} = P_{\text{abs}} - P_{\text{atm}}$	gauge pressure
$P_{\rm vac} = P_{\rm atm} - P_{\rm abs}$	vacuum pressure
$P_{\rm abs} = P_{\rm atm} + P_{\rm gage}$	absolute pressure

✤ Nomenclature

$P_{\rm abs}$	absolute pressure
P_{gage}	gage pressure
$P_{\rm vac}$	vacuum pressure
Patm	atmospheric pressure

Pressure Head:-

pressure head is the internal energy of a fluid due to the pressure exerted on its container. It may also be called **static pressure head** or simply **static head** (but not **static head pressure**). It is mathematically expressed as:

$$\Psi = \frac{p}{\gamma} = \frac{p}{\rho g}$$

where

 ψ is pressure head (<u>Length</u>, typically in units of m);

 ψ *p* is fluid <u>pressure</u> (force per unit <u>area</u>, often as <u>Pa</u> units); and

 γ is the <u>specific weight</u> (force per unit <u>volume</u>, typically N/m³ units)

 ρ is the <u>density</u> of the fluid (<u>mass</u> per unit <u>volume</u>, typically kg/m³)

g is <u>acceleration due to gravity</u> (rate of change of velocity, given in m/s²)

If intensity of pressure express in terms of height of liquid column, which causes pressure is also called pressure head.

Mathematically, h = P/w

Pressure Gauges :-

The pressure of a fluid is measured by the following devices:-

- 1. manometers
- 2. mechanical gauges

Manometers:-Manometers are defined as the devices used for measuring the pressure at a point in a fluid by balancing the column of fluid by the same or another column of the fluid. They are classified as:

- a) Simple manometers
- b) Differential manometer

9

Mechanical gauges:-mechanical gauges are defined as the devices used for measuring the pressure by balancing the fluid column by the spring or dead weight. The commonly used mechanical gauges are:-

- a) Diaphragm pressure gauge
- b) Bourdon tube pressure gauge
- c) Dead weight pressure gauge
- d) Bellows pressure gauge

PRESSURE EXERTED ON IMMERSED SURFACE:-

Hydrostatic forces on surfaces:-

Hydrostatic means the study of pressure exerted by a liquid at rest. The direction of such pressure is always perpendicular to the surface to which it acts.

Forces on Submerged Surfaces in Static Fluids

These are the following features of statics fluids:-

- Hydrostatic vertical pressure distribution
- Pressures at any equal depths in a continuous fluid are equal
- Pressure at a point acts equally in all directions (Pascal's'law).
- Forces from a fluid on a boundary acts at right angles to that boundary.

Fluid pressure on a surface:-

Pressure is defined as force per unit area. If a pressure p acts on a small area δA Then the force exerted on that area will be

 $F = p \delta A$

TOTAL PRESSURE:-

Total pressure is defined as the force exerted by a static fluid on a surface when the fluid comes in contact with the surface.

Mathematically total pressure,

 $P = p_1 a_1 + p_2 a_2 + p_3 a_3$

Where,

- $p_1, p_2, p_3 =$ Intensities of pressure on different strips of the surface, and
- $a_1, a_2, a_3 =$ Areas of corresponding strips.

The position of an immersed surface may be,

- Horizontal
- Vertical
- Inclined

Total Pressure On A Horizontal Immersed Surface

Consider a plane horizontal surface immersed in a liquid as shown in figure 1.

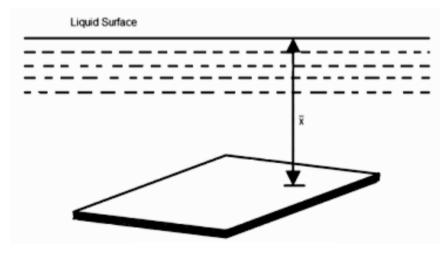


Fig. 1.3

- ω =Specific weight of the liquid
- A = Area of the immersed surface in in²
- χ = Depth of the horizontal surface from the liquid level in meters

We know that the **Total pressure** on the surface,

 \mathbf{P} = Weight of the liquid above the immersed surface

= Specific weight of liquid * Volume of liquid

= Specific weight of liquid * Area of surface * Depth of liquid

 $= \omega A \chi k N$

Total Pressure On A Vertically Immersed Surface

Consider a plane vertical surface immersed in a liquid shown in figure 2.

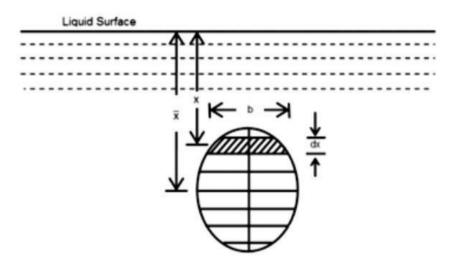


Fig. 1.4

Let the whole immersed surface is divided into a number of small parallel stripes as shown in figure.

Here,

- ω = Specific weight of the liquid
- A = Total area of the immersed surface
- χ = Depth of the center of gravity of the immersed surface from the liquid surface

Now, consider a strip of thickness dx, width b and at a depth x from the free surface of the liquid.

The intensity of pressure on the strip = $\omega \chi$

and the area of strip = b.d*x*

Pressure on the strip = Intensity of pressure * Area = $\omega \chi$.bdx

Now, Total pressure on the surface,

$$P = \int wx.bdx$$
$$= w \int x.bdx$$

11

But, $w \int x \cdot b \, dx =$ Moment of the surface area about the liquid level = Ax^{-1}

 $\therefore P = wA\overline{x}$

FLOTATION AND BUOYANCY:-

Archimedes Principle:-

Archimedes' 'rinciple indicates that the upward buoyant force that is exerted on a body immersed in a fluid, whether fully or partially submerged, is equal to the weight of the fluid that the body displaces. Archimedes' 'rinciple is a law of physics fundamental to fluid mechanics. Archimedes of Syracuse formulated this principle, which bears his name. **Buoyancy:-**

When a body is immersed in a fluid an upward force is exerted by the fluid on the body. This is upward force is equal to weight of the fluid displaced by the body and is called the force of buoyancy or simple buoyancy.

Centre of pressure:-

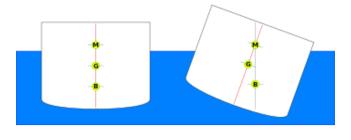
The center of pressure is the point where the total sum of a pressure field acts on a body, causing a force to act through that point. The total force vector acting at the center of pressure is the value of the integrated pressure field. The resultant force and center of pressure location produce equivalent force and moment on the body as the original pressure field. Pressure fields occur in both static and dynamic fluid mechanics. Specification of the center of pressure, the reference point from which the center of pressure is referenced, and the associated force vector allows the moment generated about any point to be computed by a translation from the reference point to the desired new point. It is common for the center of pressure to be located on the body, but in fluid flows it is possible for the pressure field to exert a moment on the body of such magnitude that the center of pressure is located outside the body.

Center of buoyancy:-

It is define as the point through which the force of buoyancy is supposed to act. As the force of buoyancy is a vertical force and is equal to the weight of the fluid displaced by the body, the center of buoyancy will be the center of gravity of the fluid displaced.

METACENTER:-

The metacentric height (GM) is a measurement of the initial static stability of a floating body. It is calculated as the distance between the centre of gravity of a ship and its metacentre. A larger metacentric height implies greater initial stability against overturning. Metacentric height also has implication on the natural period of rolling of a hull, with very large metacentric heights being associated with shorter periods of roll which are uncomfortable for passengers. Hence, a sufficiently high but not excessively high metacentric height is considered ideal for passenger ships.





The metacentre can be calculated using the formulae:

KM = KB + BM $BM = \frac{I}{V}$

Metacentric height:-

The distance between the meta-center of a floating body and a center of gravity of the body is called metacentric height.

Stability of a submerged body:-

Stable condition:-

• For stable condition $w = f_b$ and the point "B" above the CG of the body. Unstable equilibrium;-

• For unstable equilibrium $w = f_b$ and the point B is below the CG of the body. Neutral equilibrium:-

✤ If the force of buoyancy is act as CG of the body.

Stability of a floating body:-

- For stable condition $w = f_b$ and the meta centre "*m*" is about the CG of the body.
- For unstable equilibrium $w = f_b$ and the metacentre "*m*" is below CG of the body.
- In neutral equilibrium $w = f_b$ and metacentre "m" is acting at CG of the body.

Chapter-II

KINEMATICS OF FLUID FLOW

Basic equation of fluid flow and their application:-

Energy of a Liquid in Motion:-

The energy, in general, may be defined as the capacity to do work. Though the energy exits in many forms, yet the following are important from the subject point of view:

- 1. Potential energy,
- 2. Kinetic energy, and
- 3. Pressure energy.

Potential Energy of a Liquid Particle in Motion:-

It is energy possessed by a liquid particle by virtue of its position. If a liquid particle is Zm above the horizontal datum (arbitrarily chosen), the potential energy of the particle will be Z metre-kilogram (briefly written as mkg) per kg of the liquid. The potential head of the liquid, at

point, will be Z metres of the liquid.

Kinetic Energy of a Liquid Particle in Motion:-

It is the energy, possessed by a liquid particle, by virtue of its motion or velocity. If a liquid particle is flowing with a mean velocity of v metres per second; then the kinetic energy of the particle will be $V^2/2g$ mkg per kg of the liquid. Velocity head of the liquid, at that velocity, will be $V^2/2g$ metres of the liquid.

Pressure Energy of a Liquid Particle in Motion:-

It is the energy, possessed by a liquid particle, by virtue of its existing pressure. If a liquid particle is under a pressure of p kN/M2 (i.e., kPa), then the pressure energy of the

particle-will be $\frac{p}{w}$ mkg per kg of the liquid, where w is the specific weight of the

liquid. Pressure head of the liquid

under that pressure will be $\frac{p}{w}$ metres of the liquid.

Total Energy of a Liquid Particle in Motion:-

The total energy of a liquid, in motion, is the sum of its potential energy, kinetic energy and pressure energy, Mathematically total energy,

$$E = Z + V^2/2g + \frac{p}{w}$$
 m of Liquid

Total Head of a Liquid Particle in Motion:-

The total head of a liquid particle, in motion, is the sum of its potential head, kinetic head and pressure head. Mathematically, total head,

$$H = Z + \frac{V^2}{2g} + \frac{p}{w} \text{ m of liquid.}$$

Example

Water is flowing through a tapered pipe having end diameters of 150 mm and 50 mm respectively. Find the discharge at the larger end and velocity head at the smaller end, if

the velocity of water at the larger end is 2 m/s. Solution. Given: $d_1 = 150mm = 0.15 m$; $d_2 = 50 mm = 0.05 m$ and $V_1 = 2.5 m/s$. Discharge at the larger end We know that the cross-sectional area of the pipe at the larger end,

$$a_{1} = \frac{\pi}{4} \times (0.15)2 = 17.67 \times 10^{-3} \text{m}^{2}$$

and discharge at the larger end, $Q_1 = a_1.v_1 = (17.67 \times 10^{-3}) \times 2.5 = 44.2 \times 10^{-3} \text{ m}^3/\text{s}$

= 44.2Jitres/s Ans.

Velocity head at the smaller end

We also know that the cross-sectional area of the pipe at the smaller end,

$$A_2 = \frac{\pi}{4} \times (0.15)2 = 1.964 \times 10^{-3} \text{m}^2$$

Since the discharge through the pipe is continuous, therefore

or
$$v_2 = \frac{a_1.v_1}{a_2} = [(17.67 \times 10^{-3}) \times 2.5]/1.964 \times 10^{-3} = 22.5 \text{ m/s}$$

:. Velocity head at the smaller end $V_2^2/2g = (22.5)^2/2 \ge 9.81 = 25.8 \ m$ Ans

Bernoulli's Equation:-

It states, "For a perfect incompressible liquid, flowing in a continuous stream, the total nergy; of a particle remains the same, while the particle moves from one point to another." This statement is based on the assumption that there are no "losses due to friction in the pipe. Mathematically,

$$Z + V2/2g + \frac{p}{w} = Constant$$

where

Z = Potential energy, $V^2/2g$ =Kinetic energy, and $\frac{p}{w}$ = Pressure energy.

Proof

Consider a perfect incompressible liquid, flowing through a non-uniform pipe as shown in Fig-

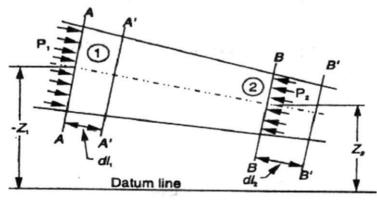


Fig. 2.1

Let us consider two sections AA and BB of the pipe. Now let us assume that the pipe is running full and there is a continuity of flow between the two sections.

Let

 Z_1 = Height of AA above the datum,

 P_1 = Pressure at AA,

 V_1 = Velocity of liquid at AA,

 A_1 = Cross-sectional area of the pipe at AA, and

 Z_2, P_2, V_2, A_2 = Corresponding values at BB.

Let the liquid between the two sections AA and BB move to A' "'nd B' "'hrough very small lengths dl_1 and dl_2 as shown in Fig. This movement of the liquid between AA and BB is equivalent to the movement 'o' the liquid between AA and A' "' 'o BB and B' ",'the remaining liquid between A' "' nd BB being un horoughlyLet W be the weight of the liquid between AA and A' ".'Since the flow is continuous, therefore

 $W = wa_1 dI_1 = wa_2 dL_2$ $a_{1 X} dl_{1} =$ or ..I) Similarly $a_2 dl_2 = \frac{W}{L}$ $a_1 dL_1 = a_2 dL_2$...Ii) We know that work done by pressure at AA, in moving the liquid to A' " ' Force x Distance $= P_1 \cdot a_1 \cdot dL_1$ Similarly, work done by pressure at BB, in moving the liquid to B' "-P₂a₂dl₂ ... Linus sign is taken as the direction of P_2 is opposite to that of P_1) :. Total work done by the pressure $= P_1 a_1 d_1 - P_2 a_2 d_2$ $=P_1a1dl_1-p_{2a}1dl_1$ \dots (a₁dl₁=a₂dl₂) $\dots (a_1 dl_1 = a_2 dl_2) = \frac{W}{W} (P_1 - P_2) \dots (a_1 dl_1 = \frac{W}{W})$ Loss of potential energy $= W (Z_1-Z_2)$ and again in kinetic energy =W[(V₂²/2g)-(V₁²/2g)] = $\frac{W}{2g}(v_2^2 - v_1^2)$

We know that loss of potential energy + Work done by pressure

= Gain in kinetic energy $\therefore W(Z_1-Z_2) + \frac{W}{w}(P_1 - P_2) = \frac{W}{2g}(v_2^2-v_1^2)$ $(Z_1-Z_2) + (p_1/w) - (p_2/w) = v_2^2/2g - v_1^2/2g$ Or $Z_1 + v_1^2/2g + (p_1/w) = Z_2 + v_2^2/2g + (p_2/w)$ which proves the Bernoulli's' equation.

Euler's' Equation For Motion

The "E" ler's' equation for steady flow of an ideal fluid along a streamline is based on the

Newton's' Second Law of Motion. The integration of the equation gives Bernoulli's' equation in the form of energy per unit weight of the flowing fluid. It is based on the 'f'llowing assumptions:

1. The fluid is non-viscous (i.e., the frictional losses are zero).

2. The fluid is homogeneous and incompressible (i.e., mass density of the fluid is constant).

3. The flow is continuous, steady and along the streamline.

4. The velocity of flow is uniform over the section.

5. No energy or force (except gravity and pressure forces) is involved in the flow.

Consider a steady' 'low of an ideal fluid along a streamline. Now consider a small element

AB of the flowing fluid as shown in Fig.

Let

dA = Cross-sectional area of the fluid element,

ds = Length of the fluid element,

dW = Weight of the fluid 5!1ement,

p = Pressure on the element at A,

p + dp = Pressure on the element at B, and

v = Velocity of the fluid element.

We know that the external forces tending to accelerate the fluid element in the direction of the streamline ds p+dp

Fig. 2.2

= p. dA - (p + dp) dA= -dp.dA

we also know that the weight of the fluid element,

 $dW = \rho g. dA . ds$

From the geometry of the figure, we find that the component of the weight of the fluid element

, in the direction of flow

= - ρ g. dA. ds cos θ dz dz $...\cos\theta = \overline{ds}$ $= - \rho g \cdot dA \cdot ds(\overline{ds})$ $= - \rho g. dA. dz$: mass of the fluid element $= \rho$.dA.Ds ,We see that the acceleration of the fluid element $\frac{dv}{dt} = \frac{dv}{ds} \times \frac{ds}{dt} = v \cdot \frac{dv}{ds}$ Now, as per Newton's' Second Law of Motion, we know that Force = Mass x Acceleration $(-dp \cdot dA) - (\rho g \cdot dA \cdot dz) = \rho \cdot dA \cdot ds^{\times} \frac{dz}{ds}$ $\frac{dp}{\rho} + g.dz = v.dv$...(dividing both side by ρdA) $Or \frac{dp}{\rho} + g.dz + v.dv = \mathbf{0}$

This is the required Euler's' equation for motion and is in the form of a differential equation. Integrating the above equation,

 $\frac{1}{\rho} + \frac{1}{g_z + v^2/2 = \text{constant}}$ $\frac{p}{w} + Z + \frac{v^2}{2g} = \text{constant} \text{ (Dividing by w)}$ or in other words, $\frac{p1}{w} + Z_1 + (v_1^2/2g) = \frac{p2}{w} + Z_2 + (v_2^2/2g)$ which proves the Bernoulli's' equation.

Limitations of Bernoulli's' Equation:-

The Bernoulli's' theorem or Bernoulli's' equation has been derived on certain assumptions, which are rarely possible. Thus the Bernoulli's' theorem has the following limitations:

- 1. The Bernoulli's' equation has been derived under the assumption that the velocity of every liquid particle, across any cross-section of a pipe, is uniform. But, in actual practice, it is not so. The velocity of liquid particle in the centre of a pipe is maximum and gradually decreases towards the walls of the pipe due to the pipe friction. Thus, while using the Bernoulli's' equation, only the mean velocity of the liquid should be taken into account.
- 2. The Bernoulli's' equation has been derived under the assumption that no external force, except the gravity force, is acting on the liquid. But, in actual practice, it is not so. There are always some external forces (such as pipe friction etc.) acting on the liquid, which effect the flow of the liquid. Thus, while using the Bernoulli's' equation, all such external forces should be neglected. But, ifsorne energy is supplied to, or, extracted from the flow, the same should also be taken into account.
- 3. The Bernoulli's' equation has been derived, under the assumption that there is. no loss of energy of the liquid particle while flowing. But, in actual practice, -it is rarely so. In a turbulent flow, some kinetic energy is converted into heat energy. And in a viscous flow, some energy is lost due to shear forces. Thus, while using Bernoulli's' equation, all such losses should be neglected.
- 4. If the liquid is flowing in a curved path, the energy due to centrifugal force should also be taken into account.

Example

The diameter of a pipe changes from 200 mm at a section 5 metres-above datum = to 50 mm at a section 3 metres above datum. The pressure of water at first section is 500 kPa. If the velocity of flow at the first section is 1 m/s, determine the intensity of pressure at the second section.

Solution.'G'~en: d_1 = 200 mm = 0.2 m; Z_1 = 5 m; d_2 = 50 mm = 0.05 m z_2 = 3 m; p = 500/

kPa = 500 kN/M2 and $V_1 = 1 mls$.

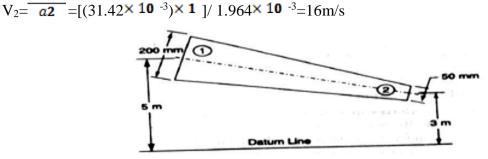
Let

 V_2 = Velocity of flow at section 2, and

P₂ = Pressure at section 2. We know that area of the pipe at section 1 $a_1 = \frac{\pi}{4} \times 0.2^2 = 31.42 \times 10^{-3} \text{m}^2$

and area of pipe at section 2 $a_1 = \frac{\pi}{4} \times 0.05^2 = 1.964 \times 10^{-3} \text{m}^2$

Since the discharge through the pipe is continuous, therefore a_1 . $V_1 = a_2$. V_2 a1. v1





Applying Bernoulli's' equation for both the ends of the pipe, $Z_1 + v_1^2/2g + (p_1/w) = Z_2 + v_2^2/2g + (p_2/w)$

 $5+(1)^2/(2 \times 9.81) + 500/9.81 = 3+(16)^2/2X9.81 + \frac{p2}{9.81}$ P2 = 40 x 9.81 = 392.4 kN/M² = 392.4 kPa Ans

practical Applications of Bernoulli's' Equation

The Bernoulli's' theorem or Bernoulli's' equation is the basic equation which has the widest applications in Hydraulics and Applied Hydraulics. Since this equation is applied for the derivation

of many formulae, therefore its clear understanding is very essential. Though the Bernoulli's' equation has a number of practical applications. yet in this chapter we shall discuss its applications on the following 'hydraulic devices :

- 1. Venturi meter.
- 2. Orifice meter.
- 3. Pitot tube.

Venturimeter

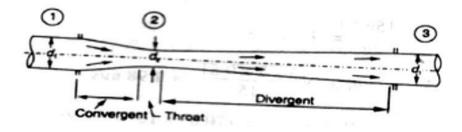


Fig. 2.4

A ve horougeter is an apparatus for finding out the discharge of a liquid flowing in a pipe. A- venture meter, in its simplest form, consists of the following three parts:

- (a) Convergent cone.
- (b) Throat.
- ©Convergent cone.
- (a) Convergent cone

It is a short pipe which converges from a diameter d_1 (diameter of the pipe. in which the venture meter is fitted) to a smaller diameter d_2 : The convergent cone is also known as inlet of the ve horougeter. The slope of the converging sides is between 1 in 4 or 1 in 5 as shown in Fig.

(b) Throat

It is a small portion of circular pipe in which the diameter d_2 is kept constant as shown in Fig.

(c) Divergent cone

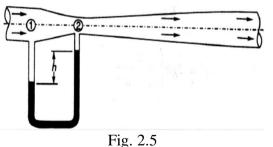
It is a pipe, which diverges from a diameter d_2 to a large diameter d_1 . The divergent cone is also known as outlet of the venture meter. The length of the divergent cone is about 3 to 4 times than that of the convergent cone as shown in Fig.

A little consideration will show that the liquid, while flowing through the venture meter, is accelerated between the sections 1 and 2 (i.e., while flowing through the convergent cone). As a result of the acceleration, the velocity of liquid at section 2 (i.e., at the throat) becomes higher than that at section 1. This increase in velocity results in considerably decreasing the pressure at section 2.1fthe pressure head at the throat falls below the separation head (which is 2.5 metres of water), then there will be a tendency of separation of the liquid flow. In order to avoid the tendency of separation at throat, there is always a fixed ratio of the diameter of throat and the pipe (i.e., dz/dt). This ratio varies from 1/4 to 3/4, but the most suitable value is 1/3 to 1/2.

The liquid, while flowing through the venture meter, is decelerated (i.e., retarded) between the sections 2 and 3 (i.e., while flowing through the divergent cone). As a result of this retardation, the velocity of liquid decreases which, consequently, increases the pressure. If the pressure is rapidly recovered, then there is every possibility for the stream of liquid to break away from the walls of the metre due to boundary layer effects. In order to avoid the tendency of breaking away the stream of liquid, the divergent cone is made sufficiently longer. Another reason for making the divergent cone longer is to mi horoughthe frictional losses. Due to these reasons, the divergent cone is 3 to 4 times longer than convergent cone as shown in Fig.

Discharge through a Venturi meter

Consider a venture meter through which some liquid is flowing as shown in Fig.



Let

 P_1 = Pressure at section 1,

 V_1 = Velocity of water at section 1,

 $Z_1 =$ Datum head at section 1,

 a_1 = Area of the ve horougeter at section 1, and

 $p_2, v_2, z_2, a_2 =$ Corresponding values at section 2.

 $Z_1 + v_1^2/2g + (p_1/w) = Z_2 + v_2^2/2g + (p_2/w).$ (1)

Let us pass our datum line through the axis of the venture meter as shown in Fig. Now $Z_1=0$ and $Z_2=0$

•
$$v_1^2/2g + (p_1/w) = v_2^2/2g + (p_2/w)$$

Or $(p_1/w)-(p_2/w)=v_2^2/2g-v_1^2/2g.$ (2)

Since the discharge at sections 1 and 2 is continuous, therefore

$$V_{1}=a_{2}v_{2}/a_{1} (a_{1}v_{1}=a_{2}v_{2})$$

$$V_{1}^{2}=a_{2}^{2}v_{2}^{2}/a_{1}^{2}$$
(3)

Substituting the above value of v_1^2 in equation (2),

$$\frac{p\mathbf{1}}{w} - \frac{p\mathbf{2}}{w} = v_2^2/2g \cdot (a_2^2/a_1^2 X v_2^2/2g)$$
$$= v_2^2/2g(1 - a_2^2/a_1^2) = v_2^2/2g[(a_1^2 - a_2^2)/a_1^2]$$
$$p\mathbf{1} \quad p\mathbf{2}$$

We know that $\overline{w} - \overline{w}$ is the difference between the pressure heads at sections 1 and 2 when the pipe is horizontal, this difference represents the ve horougead and is denoted by b

Or
$$h = v_2^2/2g[(a_1^2 - a_2^2)/a_1^2]$$

Or $v_2^2 = 2gh[a_1^2/(a_2^2 - a_2^2)]$
 $\therefore v_2 = \sqrt{2gh}[a_1/\sqrt{a_2^2}(a_1^2 - a_2^2)]$

We know that the discharge through a venture meter,

Q = Coefficient of ve horougeter x $a_2 v_2$

=C.a₂v₂=[Ca₁a₂/
$$\sqrt{(a_1^2-a_2^2)}$$
]× $\sqrt{2gh}$

Example

A venture meter with a 150 mm diameter at inlet and 100 mm at throat is, laid with its axis horizontal and is used for measuring the flow of oil specific gravity O.9. The oil-mercury differential manometer shows a gauge difference of 200 mm. Assume coefficient of the metre as O.9 Calculate the discharge in litres per minute.

Solution. Given: $d_1 = 150 \text{ mm} = 0.15 \text{ m}; d_2 = 100 \text{ mm} = 0.1 \text{ rn};$ Specific gravity of oil = 0.9 h = 200 mm = 0.2 m of mercury and C = 0.98.

We know that the area at inlet,

$$a_1 = \frac{\pi}{4} \times 0.15^2 = 17.67 \times 10^{-3} \text{ m}^2$$

and the area at throat,

 $a_2 = \frac{\pi}{4} \times 0.1 \ {}^2 = 7.854 \times 10^{-3} \mathrm{m}^2$

We also know that the difference of pressure head, H=0.2(13.6-0.9/0.9)=2.82 m of oil and the discharge through the ve horougeter,

Q= $[Ca_1a_2/\sqrt{(a_1^2-a_2^2)}] \times \sqrt{2gh}$ =63.9 X 10⁻³m³/s=63.9lit/s Ans.

Orifice Metre

An orifice metre is used to measure the discharge in a pipe. An orifice metre, in its simplest

form, consists of a plate having a sharp edged circular hole known as an orifice. This plate is fixed inside a pipe as shown in Fig. c A mercury manometer is inserted to know the difference

of pressures between the pipe an? the throat (i.e., orifice). Let

h = Reading of the mercury manometer,

 $P_1 = Pressure at inlet,$

 $V_1 =$ Velocity of liquid at inlet,

 a_1 = Area of pipe at inlet, and

 P_2, v_2, a_2 = Corresponding values

at the throat.

Now applying Bernoulli's' equation for inlet of the pipe and the throat,

$$Z_1 + v_1^2/2g + (p_1/w) = Z_2 + v_2^2/2g + (p_2/w) \qquad \dots \dots \dots (i)$$

$$(p_1/w)-(p_2/w)=v_2^2/2g-v_1^2/2g$$

Or
$$h = v_2^2/2g - v_1^2/2g = 1/2g(v_2^2 - v_1^2)$$

Since the discharge is continuous, therefore $a_1.v_1 = a_2v_2$

$$V_1 = a_2/a_1 X v_2$$
 or $v_1^2 = a_2^2/a_1^2 X v_2^2$

Substituting the above value of v_1^2 in equation (ii)

$$h = 1/2g(v_2^2 - a_2^2/a_1^2 X v_2^2) = v_2^2/2g X (1 - a_2^2/a_1^2) = v_2^2/2g[(a_1^2 - a_2^2)/a_1^2]$$

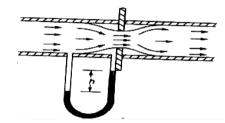
•
$$v_2^2 = 2gh[a_1^2/(a_1^2 - a_2^2)] \text{ or } v_2 = \sqrt{2}gh[a_1/\sqrt{(a_1^2 - a_2^2)}]$$

We know that the discharge,

Q = Coefficient of orifice metre x $a_2 \cdot v_2$

 $= [C\sqrt{a_1a_2}/\sqrt{a_1^2-a_2^2}] \times \sqrt{2gh}$

Example. An orifice metre consisting of 100 mm diameter orifice in a 250 mm diameter pipe has coefficient equal to 0.65. The pipe delivers oil (sp. gr. 0.8). The pressure difference on the two sides of the orifice plate is measured by a mercury oil differential inano meter. If the differential gauge reads 80 mm of mercury, calculate the rate of flow in litres.



.....(ii)



Solution. Given: $d_2 = 100 \text{ mm} = 0.1 \text{ m}; d_1 = 250 \text{ mm} = 0.25 \text{ m}; C = 0.65$; Specific gravity of oil = 0.8 and h = 0.8 m of mercury.

We know that the area of pipe,

$$a_1 = \frac{\pi}{4} \times 0.25^2 = 49.09 \times 10^{-3} \text{ m}^2$$

and area of throat

$$a_2 = \frac{\pi}{4} \times 0.1^2 = 7.854 \times 10^{-3} \text{m}^2$$

We also know that the pressure difference,

h = 0.8[(13.6-0.8)/0.8]=12.8 m of oil

and rate of flow,

$$Q = [C\sqrt{a_1a_2}/\sqrt{a_1a_2}] \times \sqrt{2gh}$$

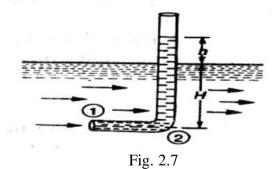
=82 × 10⁻³ m³/s=82 lit/s Ans

Pitot Tube.

A Pitot tube is an instrument to determine the velocity of flow at the required point in a pipe or a stream. In its simplest form, a pitot tube consists of a glass tube bent a through 90° as shown in Fig.

The lower end of the tube faces the direction of the flow as shown in Fig. The liquid rises up in the tube due to the pressure exerted by the flowing liquid. By measuring the rise of liquid in the tube, we can find out the velocity of the liquid flow.

Let h = Height of the liquid in the pitot tube above the surface,



H = Depth of tube in the liquid, and

v = Velocity of the liquid.

Applying Bernoulli's' equation for the sections 1 and 2, $H+v^2/2g=H+h$

.....(z₁=z₂)

$$h = v^2/2g$$

∴ v = √2gh

Example.

A pltot tube was inserted in a pipe to measu!e the velocity of water in it. If (

water rises the tube is 200 mm, find the velocity of water.

Solution. Given: h = 200 mm = 0.2 m.

We know that the velocity of water in the pipe,

 $v = \sqrt{2}gh = \sqrt{2}(2 \times 9.81 \times 0.2) = 1.98 \text{ m/s}$ Ans.

Rate of Discharge

The quantity of a liquid, flowing per second through a section of a pipe or a channel, is known as the rate of discharge or simply discharge. It is generally denoted by Q. Now consider a liquid flowing through a pipe.

Let, a = Cross-sectional area of the pipe, and v = Average velocity of the liquid,
Discharge, Q = Area × Average velocity = a.v

Notes: 1. If the area is in m^2 and velocity in m/s, then the discharge,

 $Q = m^2 x m/s = m^3/s = cumecs$ 2.member that $1m^3 = 1000$ litres.

Equation of Continuity of a Liquid Flow

If an incompressible liquid is continuously flowing through a pipe or a channel (whose cross- sectional area may or may not be constant) the quantity of liquid passing per second is the same at all sections. This is known as the equation of continuity of a liquid flow. It is the first and fundamental equation of flow.

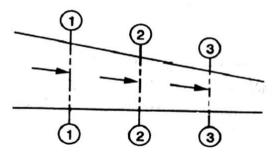


Fig. 2.8

CONTINUITY OF A LIQUID FLOW

Consider a tapering pipe through which some liquid is flowing as shown in Fig

Let , $a_1 = Cross$ -sectional area of the pipe at section 1-1, and $v_1 = Velocity$ of the liquid at section 1-1,

Similarly, a_2, v_2 = Corresponding values at section 2-2, and a_3, v_3 = Corresponding values at section 3-3. We know that the total quantity of liquid passing through section 1-1, $Q_1 = a_1.v_1$(i) Similarly, total quantity of liquid passing through section 2-2, $Q_2 = a_1.v_1$(ii) and total quantity of the liquid passing through section 3-3, $Q_3 = a_3.v_3$(iii)

From the law of conservation of matter, we know that the total quantity of liquid passing through the sections 1-1, 2-2 and 3-3 is the same. Therefore $Q_1 = Q_2 = Q_3 = \dots$ or a_1 . $v_1 = a_2$. $v_2 = a_3$. v_3 and so on.

Example : Water is flowing through a pipe of 100 mm diameter with an average velocity 10 m/s. Determine the rate of discharge of the water in litres/s. Also determine the velocity of water

At the other end of the pipe, if the diameter of the pipe is gradually changed to 200 mm.

Solution. Given: $d_1 = 100 \text{ mm} = 0.1 \text{ m}$; $V_1 = 10 \text{ m/s}$ and $d_2 = 200 \text{ mm} = 0.2 \text{ m}$. *Rate of discharge*

We know that the cross-sectional area of the pipe at point 1,

$$a_1 = \sqrt{4} x(0.1)^2 = 7.854 \times 10^{-3} \text{ m}^2$$

and rate of discharge, $Q = a_{1.}v_{1} = (7.854 \text{ x } 10^{-3})\text{x} \quad 10 = 78.54 \text{ X } 10^{-3} \text{ m}^{3}/\text{s}$

= 78.54 litres/s **Ans.**

Velocity of water at the other end of the pipe

We also know that cross-sectional area of the pipe at point 2,

$$a_2 = (\frac{\pi}{4})_{x(0.2)^2 = 31.42 \times 10^{-3} \text{ m}^2}$$

and velocity of water at point 2, $v_2 = \overline{a2} = ((78.54 \text{ X } 10^{-3})/(31.42 \text{ x} 10^{-3})) = 2.5 \text{ m/s}$ Ans.

Flow over Notches:-

A notch is a device used for measuring the rate of flow of a liquid through a small channel or a tank. It may be defined as an opening in the side of a tank or a small channel in such a way that the liquid surface in the tank or channel is below the top edge of the opening.

A weir is a concrete or masonry structure, placed in an open channel over which the flow occurs. It is generally in the form of vertical wall, with a sharp edge at the top, running all the way across the open channel. The notch is of small size while the weir is of a bigger size. The notch is generally made of metallic plate while weir is made of concrete or masonry structure.

- 1. Nappe or Vein. The sheet of water flowing through a notch or over a weir is called Nappe or Vein.
- 2. Crest or Sill. The bottom edge of a notch or a top of a weir over which the water flows, is known as the sill or crest.

Classification Of Notches And Weirs:-

The notches are classified as :

- I. According to the shape of the opening:
- (a) Rectangular notch,
- (b) Triangular notch,
- (c) Trapezoidal notch, and
- (d) Stepped notch.
- 2. According to the effect of the sides on the nappe:
- (a) Notch with end contraction.
- (b) Notch without end contraction or suppressed notch,

Weirs are classified according to the shape of the opening , the' shape of the crest, the effect of the sides on the nappe and nature of discharge. The following are important classifications.

Discharge Over A Rectangular Notch Or Weir

The expression for discharge over a rectangular notch or weir is the same.

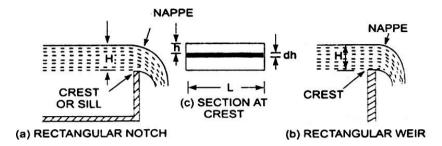


Fig. 2.9

Rectangular notch and weir:-

Consider a rectangular notch or weir provided in a channel carrying water as shown in Fig Let H = Head of water over the crest L = Length of the notch or weir

The total discharge,
$$Q = \frac{2}{3} \times \frac{L}{c_d} \times L \times \sqrt{2g[H]}_{3/2}$$

Problem - -

Find the discharge of water flowing over a rectangular notch 0/2 In length when the constant head over the notch is 300 mm. Take cd = 0.60. Solution. Given:

Length of the notch, L=2.0m Head over notch, H = 300 m = 0.30 mC_d=0.06

Discharge
$$Q = \frac{2}{3} \times c_d \times L \times \sqrt{2g[H]_{3/2}}$$

$$=\frac{2}{3} \times 0.6 \times 2.0 \times \sqrt{2} \times 9.81 \times [0.30]_{1.5 \text{ m}3/\text{s}}$$

= 3.5435 x 0.1643 = 0.582 m3/s. Ans, **Problem 2**

Determine the height of a rectangular weir of length 6 m to be built across a Rectangular channel. The maximum depth of water on the upstream side of the weir is 1.8m and discharge is 2000 litres/s. Take Cd = 0.6 and neglect end contractions.

Solution. Given:

Length of weir, L=6m

Depth of water, H1=1.8m

Discharge, Q = 2000 litIs = 2 m3/s

Cd = 0.6

Let H is the height of water above the crest of weir and H2 =height of weir The discharge over the weir is given by the equation .

$$Q = \frac{2}{3} \times c_d \times L \times \sqrt{2g[H]}_{3/2}$$
$$2 = \frac{2}{3} \times 0.6 \times 6 \times \sqrt{2} \times 9.81 \times [H]_{3/2}$$

=10.623 H^{3/2}

⁼ H^{3/2}=10.623

$$H = \left(\frac{2.0}{10.623}\right)_{2/3} = 0.328 \text{ m}$$

Height of weir, H2 = H1- H

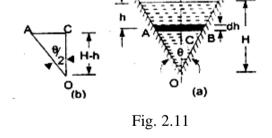
= Depth of water on upstream side - H

= 1.8 - .328 = 1.472 m. Ans.

Discharge Over A Triangular Notch Or Weir:-

The expression for the discharge over a triangular notch or weir is the same. It is derived as : Let H = head of water above the V- notch

 $\theta = \text{angle of notch}$ Total discharge, $Q = \frac{15}{15} \times C_d \times \frac{\tan \theta}{2} \times \sqrt{2g} \times H_{5/2}$ For a right angle V Notch , if $C_d = 0.6$ $\theta = 90_{0, \tan 2} = 1$ Discharge, $Q = \frac{8}{15} \times 0.6 \times 1 \times \sqrt{2 \times 9.81} \times H^{5/2}$ $= 1.417 \times H^{5/2}$



Problem -1

Find the discharge over a triangular notch of angle 60° when the head over theV-

notch is 0.3 m. Assume $C_d = 0.6$.

Solution. Given an Angle of V-notch, $e = 60^{\circ}$

Head over notch, H=0.3 m

$$C_{d} = 0.6$$

Discharge, Q over a V-notch is given by equation

$$\underset{\text{Q=15}}{\overset{\textbf{8}}{=}} \times C \underset{\text{d}}{\times} \frac{\tan \theta}{2} \times \sqrt{2g} \times H_{5/2}$$

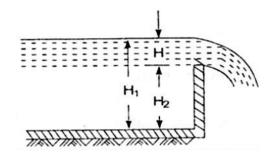


Fig. 2.10

 $\frac{8}{15} \times C_{d} \times \frac{0.6 \tan 60}{2} \times \sqrt{2 \times 9.81} \times (0.3)_{5/2}$ = 0.8182 x 0.0493 = 0.040 m3/s. Ans,

Problem -2

Water flows over a rectangular weir 1 m wide at a depth of 150 mm and afterwards passes through a triangular right-angled weir. Taking C_d for the rectangular and triangular weir as 0.62 and 0.59 respectively, find the depth over the triangular weir.

Solution. Given:

For rectangular weir. Length= L = 1 m

Depth of water, H = 150 mm = 0.15 m

 $C_d = 0.62$

For triangular weir.

$$\theta = 90^{\circ}$$

$$C_{d} = 0.59$$

Let depth over triangular weir = H₁ The discharge over the rectangular weir IS given by equation

$$Q = \frac{\mathbf{2}}{\mathbf{3}} \times c_d \times L \times \sqrt{2g[H]}_{3/2}$$
$$= \frac{\mathbf{2}}{\mathbf{3}} \times 0.62 \times 1.0 \times \sqrt{2 \times 9.81} \times (0.15)_{3/2}$$

 $=0.10635 \text{ m}^3/\text{s}$

The same discharge passes through the triangular right-angled weir. But discharge. Q. is given by the equation

$$\begin{array}{l} \frac{8}{Q=15} \times C_{d} \times \frac{\tan \theta}{2} \times \sqrt{2g} \times H_{5/2} \\
0.10635 = \frac{8}{15} \times 0.59 \times \frac{\tan 90}{2} \times \sqrt{2g} \times H_{1^{5/2}} \\
= \frac{8}{15} \times 0.59 \times 1 \times 4.429 \times H_{1^{5/2}} \\
= 1.3936 \, \text{H}_{1^{5/2}} \\
\text{H}_{1^{5/2}=1.3936} = 0.07631 \\
\text{H}_{1} = (0.07631)^{0.4} = 0.3572 \, \text{m}_{1^{5/2}} \text{Ans}
\end{array}$$

Discharge Over A Trapezoidal Notch Or Weir:-

A trapezoidal notch or weir is a combination of a rectangular and triangular notch or weir. Thus the total discharge will be equal to the sum of discharge through a rectangular weir or notch and discharge through a triangular notch or weir.

Let H = Height of water over the notch

L = Length of the crest of the notch

 C_{d1} = Co-efficient or discharge. for rectangular portioo ABCD of Fig. C_{d2} = Co-efficient of discharge for triangular portion [FAD and BCE] The-discharge through rectangular portion ABCD is given by

or
$$Q_1 = \frac{2}{3} \times C_{d1} \times L \times \sqrt{2g} \times H^{3/2}$$

The discharge through two triangular notches FDA and BCE is equal to the discharge through a single triangular notch of angle e and it is given by equation

$$\frac{2}{Q_2=3} \times C_{d2} \times \frac{\tan \theta}{2} \times \sqrt{2g} \times H_{5/2}$$

Discharge through trapezoldal notch or weir FDCEF = Q₁ + Q₂
$$\frac{2}{3} \times C_{d1} \sqrt{2g} \times H_{3/2} + \frac{8}{15} C_{d2} \times \frac{\tan \theta}{2} \times \sqrt{2g} \times H_{5/2}$$

Problem -1 Find the discharge through a trapezoidal notch which is 1 m wide at the tap and 0.40 m at the bottom and is 30 cm in height. The head of water On the notch is 20 cm. Assume C_d for rectangular portion = 0.62 while for triangular portion = 0.60.

Solution. Given: AE=1 m Top width Base width, CD=L=0.4 m Head of water, H=0.20 m For rectangular portion, $C_{d1} = 0.62$ From **ABC**, we have $\frac{\tan\theta}{2} = \frac{AB}{BC} = \frac{\frac{AE - CD}{2}}{\frac{H}{H}}$ $= \frac{\frac{1.0 - 0.4}{2}}{0.3} = \frac{\frac{0.6}{2}}{\frac{0.3}{0.3}} = \frac{0.3}{0.3} = 1$ Fig. 2.12 Discharge through trapezoidal notch is given by equation $Q = \frac{\mathbf{2}}{\mathbf{3}}C_{d1} \times L \times \sqrt{2g} \times H^{3/2} + \frac{\mathbf{8}}{\mathbf{15}}C_{d2} \times \frac{\tan\theta}{2\sqrt{2g}} \times H^{5/2}$ $=\frac{2}{3} \times 0.62 \times 0.4 \times \sqrt{2 \times 9.81} \times (0.2)^{3/2} + \frac{3}{15} \times 60 \times 1 \times \sqrt{2 \times 9.81} \times (0.2)^{5/2}$ $= 0.06549 + 0.02535 = 0.09084 \text{ m}^3/\text{s} = 90.84 \text{ litres/s}$. Ans

Discharge Over A Stepped Notch:-

A stepped notch is a combination of rectangular notches. The discharge through 'stepped notch is equal to the sum of the discharges' 'hrough the different rectangular notches.

Consider a stepped notch as shown in Fig.

Let H_1 = Height of water above the crest of notch (1).

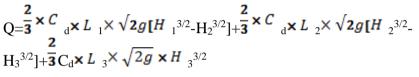
 $L_1 = Length of notch 1$,

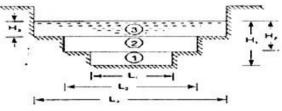
 H_{2},L_{2} and H_{3},L_{3} are corresponding values for notches 2 and 3 resp

C_d=Co-efficient of discharge for all notches

Total discharge $Q=Q_1+Q_2+Q_3$







Problem

Fig. 2.13

Fig. 1 shows a stepped notch. Find the discharge through the notch if Cd for all section = 0.62. Solution. Given: $L_1 = 40 \text{ cm}, L_2 = 80 \text{ cm},$ $L_3 = 120 cm$ $H_1 = 50 + 30 + 15 = 95 \text{ cm},$ H₂=80 cm,H₃=50 cm, $C_d = 0.62$ Total Discharge , $Q=Q_1+Q_2+Q_3$ 15 cm where $\frac{2}{Q_1 = 3} \times C_{d} \times L_1 \times \sqrt{2g[H_1^{3/2} - H_2^{3/2}]}$ $=\frac{2}{3} \times 0.62 \times 40 \times \sqrt{2 \times 981} \times [95^{3/2} - 80^{3/2}]$ $=154067 \text{ cm}^3/\text{s}$ =154.067 lit/s $Q_{2=}\frac{2}{3} \times C_{d} \times L_{2} \times \sqrt{2g[H_{2^{3/2}}-H_{3^{3/2}}]}$ $=\frac{2}{3} \times 0.62 \times 80 \times \sqrt{2 \times 981} \times [80^{3/2} - 50^{3/2}]$ $=530141 \text{ cm}^{3}/\text{s}$

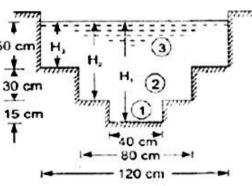


Fig. 2.14

=530.144 lit/s

$$Q_3 = \frac{2}{3}C_d \times L_3 \times \sqrt{2g} \times H_3^{3/2}$$

 $= \frac{2}{3} \times 0.62 \times 120 \times \sqrt{2 \times 981} \times 50_{3/2}$
=776771 cm³/s
=776.771 lit/s
 $\therefore Q = Q_1 + Q_2 + Q_3$
=154.067+530.144+776.771
=1460.98 lit/s Ans.

Velocity Of Approach

Velocity of approach is defined as the velocity with which the water approaches or reaches the weir or notch before it flows over it. Thus if V_a is the velocity of approach, then an additional head h_a equal

to $V_a^2/2g$ due to velocity of approach, is acting on the water. flowing over the notch. Then initial height of water over the notch becomes (H+ h_a) and final height becomes equal to h_a ,' 'hen all the formulae are

changed taking into consideration of velocity of approach.

The velocity of approach, V_a is determined by finding the discharge over the notch or weir neglecting velocity of approach. Then dividing the -d-scharge-by the cross-sectional area of the channel .on the' 'pstream side of the weir or notch, the velocity of approach is obtained . Mathematically,

This velocity of approach is used to find an additional head ($h_a = V_a^2/2g$). Again the discharge is calculated and above process is repeated for more accurate discharge. Discharge over a rectangular weir, with velocity of approach

$$= \frac{2}{3} \times C_{d} \times L \times \sqrt{2g} [(H_1 + h_a)^{3/2} - h_a^{3/2}]$$

Problem:-

Water is flowing in a rectangular channel of 1 m wide and 0.75 m deep. Find the discharge over a rectangular weir of crest length 60 cm if the head of water over the crest of weir is

32

20 cm and water from channel flows over the weir. Take Cd = 0.62. Neglect end contractions. Take

velocity of approach into consideration. Solution. Given:

Area of channel, $A = Width x depth = 1.0 \times 0.75 = 0.75 \text{ m}^2$

Length of weir, L = 60 cm = 0.6 m

Head of water, $H_1 = 20 \text{ cm} = 0.2 \text{ m}$

$$C_{d} = 0.62$$

Discharge over a rectangular weir without velocity of approach is given by

$$Q = \frac{2}{3C_{d}} \times L \times \sqrt{2g} \times H_{1^{3/2}}$$

= $\frac{2}{3} \times 0.62 \times 0.6 \times \sqrt{2 \times 9.81} \times (0.2)_{3/2}$
= 0.0982 m³/s

velocity of approach $V_a = \frac{Q}{A} = \frac{0.0982}{0.75} = 0.1309 \frac{m}{s}$ Additional head $h_a = V_a^2/2g$

 $=(0.1309)^2/2 \times 9.81 = 0.0008733 m$

Then discharge with velocity of approach is given by equation

$$Q = \frac{2}{3} \times C_{d} \times L \times \sqrt{2g} [(H_{1} + h_{a})^{3/2} - h_{a}^{3/2}]$$

= 2/3 × 0.62 × 0.6 × $\sqrt{(2 \times 9.81[(0.2 + 0.00087)^{3/2} - (0.00087)^{3/2}]}$
= 1.098 [0.09002- .00002566]

= 1.098 x 0.09017

 $=0.09881 \text{ m}^3/\text{s}$. Ans

Types of Weirs :-

Though there are numerous types of weirs, yet the following are important from the subject point of view :

- 1. Narrow-crested weirs,
- 2. Broad-crested weirs,
- 3. Sharp-crested weirs,
- 4: Ogee weirs, and
- 5. Submerged or drowned weirs.

Discharge over a Narrow-crested Weir :-

The weirs are generally classified according to the width of their crests into two types. i.e.

narrow-crested weirs and broad crested weirs.

Let b = Width of the crest of the weir, and

H = Height of water above the weir crest.

If 2b is less than H,the weir is called a narrow-crested weir. But if 2b is more than H . it is called a broad-crested weir.

A narrow-crested weir is hydraulically similar to an ordinary weir or to a rectangular weir .Thus, the same formula for discharge over a narrow-crested weir holds good, which we derived from an ordinary weir .

$$\mathbf{Q} = \mathbf{\overline{3}} \ \mathbf{X} \ \mathbf{C}_{\mathrm{d}} \ .\mathbf{L} \sqrt{\mathbf{2g}} \ \mathbf{x} \ \mathrm{H}^{3/2}$$

Where, Q = Discharge over the weir,

Cd = Coefficient of discharge,

L = Length of the weir, and

H = Height of water level above the crest of the weir.

Example A narrow-crested weir of 10metres long is discharging water under a constant head of 400 mm. Find discharge over the weir in litresls. Assume coefficient of discharge as 0.623.

Solution. Given: L = 10 m; H= 400 mm = 0.4 m and $C_d = 0.623$. We know that the discharge over the weir,

$$Q = \frac{2}{3} \times C_{d} \cdot L \sqrt{2g} \times H^{3/2}$$

= $\frac{2}{3} \times 0.623 \times 10 \sqrt{(2 \times 9.81)} \times (0.4)^{3/2}$
= 46.55 m²/s = 4655 lit/s

Discharge over a Broad-crested Weir :-

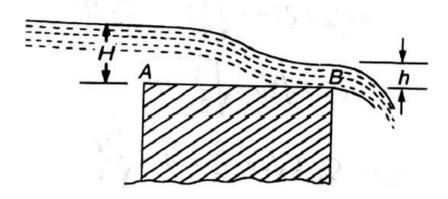


Fig. 2.15

Broad-crested weir

Consider a broad-crested weir as shown in Fig. Let A and B be the upstream and downstream ends of the weir.

Let H = Head of water on the upstream side of the weir (i.e., at A),

h = Head of water on the downstream side of the weir (i.e., at B),

v = Velocity of the water on the downstream side of the weir

(i.e., at B),

 $C_d = Coefficient$ of discharge, and

L = Length of the weir.

Q=1.71C_d .L × $H^{3/2}$

Example A broad-crested weir 20 m long is discharging water from a reservoir in to channel. What will be the discharge over the weir, if the head of water on the upstream and downstream sides is 1m and 0.5 m respectively? Take coefficient of discharge for the flow as 0.6.

Solution. Given: L = 20 m; H = 1 m; h = 0.5 m and $C_d = 0.6$. We know that the discharge over the weir, $Q = C_d \mathbf{X}$.h $\sqrt{2g(H - h)}$ = 0.6 x 2.0 x 0.5 x $\sqrt{2} \times 9.81(1 - 0.5) \text{ m}^3/\text{s}$

 $= 6 \times 3.13 = 18.8 \text{ m}^3/\text{s}$ Ans.

Discharge over a Sharp-crested Weir :-

It is a special type of weir, having a sharp-crest as shown in Fig. The water flowing over the crest comes in contact with the crest -l-ne and then springs up from the crest and falls as a trajectory as shown in Fig.

In a sharp-crested weir, the thickness of the weir is

kept less than half of the height of water on the weir. i.e.,

b<(H/2)

where , b = Thickness of the weir,

and H = Height of water, above the crest of the weir.

The discharge equation, for a sharp crested weir, remains the same as that of a rectangular weir. i.e.,

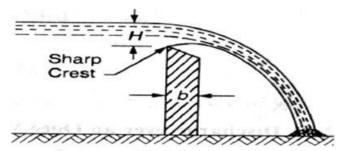


Fig. 2.16

Sharp-crested weir :-

$$Q = \frac{2}{3} X C_d . L \sqrt{2g} x H^{3/2}$$

Where, C_d = Coefficient of discharge, and L = Length of sharp-crested weir

Example In a laboratory experiment, water flows over a sharp-crested weir 200 mm long under a constant head of 75mm. Find the discharge over the weir in litres/s, if $C_d = 0.6$. **Solution.** Given: L = 200 mm = 0.2 m; H = 75 mm = 0.075 m and $C_d = 0.6$. We know that the discharge over the weir,

$$Q = \frac{2}{3} \times C_{d} . L \sqrt{2g} \times H^{3/2}$$

= $\frac{2}{3} \times 0.6 \times 0.2 \times \sqrt{2 \times 9.81} \times (0.075)_{3/2}$
= 0.0073 m³/s = 7.3 litres/s. Ans.

Discharge over an Ogee Weir :-

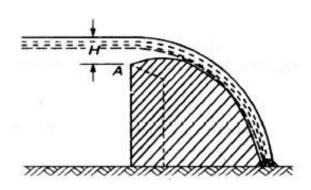
It is a special type of weir, generally, used as a spillway of a dam as shown in Fig.

, The crest of an agee weir slightly rises up from the

point A ,(i.e., crest of the sharp-crested weir) and after reaching the maximum rise of 0.115 H (where H is the height of a water above the point A) falls in a parabolic form as shown in Fig.

The discharge equation for an agee weir remains the same as that of a rectangular weir. i.e.,

 $Q = \frac{2}{3} X C_d . L \sqrt{2g} x H^{3/2}$ Where $C_d = \text{Co-efficient of discharge and}$ L= Length of an ogee weir





Example

An ogee weir 4 metres long has 500 mm head of water. Find the discharge over the weir, if $C_d = 0.62$.

Solution. Given: L = 4 m; H = 500 mm = 0.5 m and $C_d = 0.62$.

We know that the discharge over the weir,

$$Q = \frac{2}{3} X C_{d} . L \sqrt{2g} x H^{3/2}$$

$$= \frac{2}{3} X 0.62 X 4 \sqrt{2} 2 X 9.81 X (0.5)^{3/2} m^{3/s}$$

$$= 7.323 x 0.354 = 2.59 m^{3/s} = 2590 \text{ litres/s} \text{ Ans}$$

Discharge over a Submerged or Drowned Weir :-

When the water level on the downstream side of a weir is above the top surface of weir, it is known a submerged or drowned weir as shown in Fig

The total discharge, over such a weir, is found out by splitting up the height of water, above the sill of the weir, into two portions as discussed below:

Let H_1 = Height of water on the upstream side of the weir, and

 H_2 =height of water on the downstream side

of the weir.

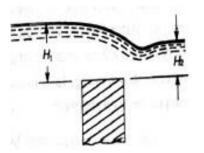


Fig. 2.18

The discharge over the upper portion may be considered as a free discharge under a head of water equal to $(H_1 - H_2)$. And the discharge over the lower portion may be considered as a submerged discharge under a head of H_2 . Thus discharge over the free portion (i.e., upper portion),

$$Q1 = \frac{2}{3} X Cd . L \sqrt{2g} x (H1-H2)^{3/2}$$

Submerged weir :-

and the discharge over the submerged (i.e., lower portion), $Q_2 = C_d \cdot L \cdot H_2 \cdot \sqrt{2g(H_1 - H_2)}$:. Total discharge, $Q = Q_1 + Q_2$

Example A submerged sharp crested weir 0.8 metre high stands clear across a channel having vertical sides and a width of 3 meters. The depth of water in the channel of approach is 1.2 meter. And 10 meters downstream from the weir, the depth of water is 1 meter. Determine the discharge over the weir in liters per second. Take C_d as 0.6.

Solution. Given: L = 3 m and Cd = 0.6.

From the geometry of the weir, we find that the depth

of water on the upstream side,

 $H_1 = 1.25 - -.8 = 0.45$ m and depth of water on the downstream side,

 $H_2 = 1 - 0.8 = 0.2 \text{ m}$

We know that the discharge over the free portion of the weir

$$Q_{I} = \frac{2}{3} X Cd . L \sqrt{2g} x (H1 - H2)^{3/2}$$

= $\frac{2}{3} \times 0.6 \times 3 \times (\sqrt{2 \times 9.81}) (0.45 - 0.20)_{3/2}$
= 5.315 x 0.125 = 0.664 m³/s = 664 liters/s ... (i)

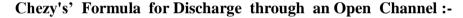
and discharge over the submerged portion of the weir,

 $Q_2 = C_d$. L. H_2 . $\sqrt{2g(H_1-H_2)}$

 $= 0.6 \times 3 \times 0.2 \sqrt{2} 2 \times 9.81(0.45-0.2) \text{ m}^{3}/\text{s}$ = 0.36 x 2.215 = 0.797 m³/s = 797 liters/s ... (ii) :. Total discharge: Q = Q₁ + Q₂ = 664 + 797 = 1461 liters/ s **Ans.**

2.3 Flow over Weirs:-

An open channel is a passage through which the water flows under the force of gravity - atmospheric pressure. Or in other words, when the free surface of the flowing water is in contact, with the atmosphere as in the case of a canal, a sewer or an aquaduct, the flow is said to be through an open channel. A channel may be covered or open at the top. As a matter of fact, the flow of water in an open channel, is not due to any pressure as in the case of pipe flow. But it is due to the slope the bed of the channel. Thus during the construction of a channel, a uniform slope in its bed is provided to maintain the flow of water.



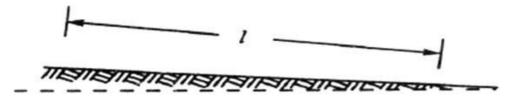


Fig. 2.19

Sloping bed of a channel :-

Consider an open channel of uniform cross-section and bed slope as shown in Fig.

Let

I = Length of the channel,

A = Area of flow,

v = Velocity of water,

p = Wetted perimeter of the cross-section, m=

f = Frictional resistance per unit area at unit velocity, and

i = Uniform slope in the bed.

$$m = \frac{A}{P}$$
(known as hydraulic mean depth or hydraulic radious)

 \therefore Discharge Q= A X v=AC $\sqrt{}$ mi

Example.

A rectangular channel is 1. 5 metres deep and 6 metres wide. Find the discharge through channel, when it runs full. Take slope of the bed as 1 in 900 and Chezy's constant as 50. Solution. Given: d = 1.5 m; b = 6 m; i = 1/900 and C = 50.

We know that the area of the channel,

 $A = b.d = 6 x 1.5 = 9 m^2$

and wetted perimeter,

D = b + 2d = 6 + (2 x 1.5) = 9 m

:. Hydraulic mean depth, $m = \frac{A}{P} = 1 m$

and the discharge through the channel,

 $Q = AC\sqrt{mi} = 9x50\sqrt{(1 X 1/900)} = 15m^{3}/s$ Ans.

Manning Formula for Discharge :-

Manning, after carrying out a series of experiments, deduced the following relation for the value of C in Chezy's' formula for discharge:

$$C = \frac{1}{N} \times m_{1/6}$$

where N is the Kutter's' constant Now we see that the velocity,

$$v = C \sqrt{m} m = M X m^{2/3} X i^{1/2}$$

where

M =1/N and is known as Manning's' constant.

Now the discharge,

Q = Area x Velocity = A x 1/N x m² xi^{1/2}

 $= A x M x m^{2/3} x i^{1/2}$

Example

An earthen channel with a 3 m wide base and side slopes 1 : 1 carries water with a depth of 1 m. The bed slope is 1 in 1600. Estimate the discharge. Take value of N in Manning's' formula as 0.04.

Solution.

Given: b = 3 m; Side slopes = 1 : 1; d = 1 m; i = 1/1600 and N = 0.04.

We know that the area of flow,

A = $\overline{2} x (3 + 5) x1 = 4 m^2$ and wetted perimeter, P = 3 + 2 X $\sqrt{(1)^2 + (1)^2} = 5.83 m$ \therefore hydraulic mean depth m = A/P=4/5.83=0.686 m

We know that the discharge through the channel

Q = Area x Velocity = A x 1/N x $m^{2/3}$ xi^{1/2} = 4 X 1/0.04 X 0.686^{2/3} X (1/1600)^{1/2} =1.945 m ³/s Ans

Channels of Most Economical Cross-sections :-

A channel, which gives maximum discharge for a given cross-sectional area and bed slope is called a channel of most economical cross-section. Or in other words, it is a channel which involves least excavation for a designed amount of discharge. A channel of most economical cross-section is, sometimes: also defined as a channel which has a minimum wetted perimeter; so that there is a minimum resistance to flow and thus resulting in a maximum discharge. From the above definitions,

it is obvious that while deriving the condition for a channel of most economical crosssection, the cross-sectional area is assumed tobe constant. The relation between depth and breadth of the section is found out to give the maximum discharge.

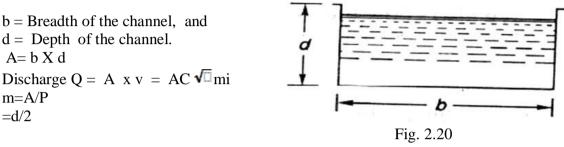
The conditions for maximum discharge for the following sections will be dealt with in the succeeding pages :

- 1. Rectangular section,
- 2. Trapezoidal section, and
- 3. Circular section.

Condition for Maximum Discharge through a Channel of Rectangular Section :-A rectangular section is, usually, not provided in channels except in rocky soils where the faces of rocks can stand vertically. Though a rectangular section is not of much practical importance, yet we shall discuss it for its theoretical importance only.

Consider a channel of rectangular section as shown in Fig.

Let



Hence, for maximum discharge or maximum velocity, these two conditions (i.e., b = 2d and

m = d/2) should be used for solving the problems of channels of rectangular cross-sections.

Example

A rectangular channel has a cross-section of 8 square metres. Find its size and discharge through the most economical section, if bed slope is 1 in 1000. Take C = 55.

Solution. Given: $A = 8 m^2$

i= 1/1000 = 0.001 and C = 55. Size of the channel Let b = Breadth of the channel, and d = Depth of the channel. We know that for the most economical rectangular section, b = 2d :. Area (A) 8=b X d= 2d X d = 2d² = b=2 m

And b=2d=2 X 2= 4 m

Discharge through the channel

We also know that for the most economical rectangular section, hydraulic mean depth,

m=d/2=2/2=1 m

and the discharge through the channel,

 $Q = AC \sqrt{mi} = 8 \times 55\sqrt{1} \times 10001 \text{ m}^3/\text{s}$ = 440 x 0.0316 = 13.9 m³/s , Ans.

Condition for Maximum Discharge through a Channel of Trapezoidal Section :-

A trapezoidal section is always provided in the earthen channels. The side slopes, in a channel of trapezoidal cross-section are provided, so that the soil can stand safely. Generally, the side slope in a particular soil is decided after conducting experiments on that soil. In a soft soil, flatter side slopes

should be provided whereas in a harder one, steeper side slopes may be provided. consider a channel of trapezoidal cross- section ABCD as shown in FIg.

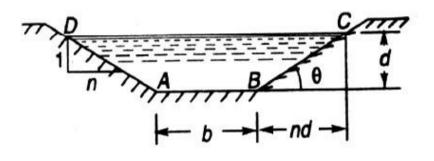


Fig. 2.21

Let b = Breadth of the channel at the bottom, d = Depth of the channel and **1** \overline{n} = side slope (i.e., 1 vertical to n horizontal)

Hence, for maximum discharge or maximum velocity these two (i.e., $b + 2nd^{/2} = d \sqrt{n^2 + 1}$ and m = d/2) should be used for solving problems on channels of trapezoidal cross-sections.

Example .

A most economical trapezoidal channel has an area of flow 3.5 m^2 discharge in the channel, when running 1 metre deep. Take C = 60 and bed slope 1 in 800.

Solution. Given: A = 3.5 m2; d = 1 m; C = 60 and i = 1/800.

We know that for the most economical trapezoidal channel the hydraulic mean depth

$$m = d/2 = 0.5 m$$

and discharge in the channel,

 $Q = A.C.\sqrt{mi} = 5.25 \text{ m}^3/\text{s}$ Ans.

Example .

A trapezoidal channel having side slopes of 1 : 1 and bed slope of 1 in 1200 is required to carry a discharge of 1800 m³/min. Find the dimensions of the channel for cross-section. Take Chezy's' constant as 50.

Solution.

Given side slope (n)=1

(i.e. 1 vertical to n horizontal),

i = 1/1200, $Q = 180m^3/min = 3m^3/sec$

and C = 50

Let b=breadth of the channel of its bottom and d= depth of the water flow.

We know that for minimum cross section the channel should be most economical and for economical trapezoidal section half of the top width is equal to the slopping side. i.e.

$$b + 2nd^{/2} = d \sqrt{n2 + 1}$$

or b = 0.828d

• Area A = d X (b + nd) = $1.828d^2$

We know that in the case of a most economical trapizodial section the hydraulic mean depth m=d/2

And discharge through the channel (Q)= A.C. \sqrt{mi} =1.866d^{5/2} \therefore d^{5/2} =3/1.866 = 1.608

Or d = 1.21 m

• b = 0.828 d = 0.828 X 1.21 = 1 m ANS
 •

Condition for Maximum Velocity through a Channel of Circular Section :-

Consider a channel 'o' circular section, discharging water under the atmospheric pressure shown in Fig.

Let

r = Radius of the channel,

h = Depth of water in the channel, and

 2θ = Total angle (in radians) subtended at the centre by the water

From the geometry of the figure, we find that the wetted perimeter of the channels,

$$\mathbf{P} = 2^{\mathbf{r} \boldsymbol{\theta}} \qquad \dots \mathbf{I}$$

and area of the section, through which the water is flowing,

 $A = r^{2} \theta - \frac{r2 \sin 2\theta}{2} = r^{2} (\theta - \frac{\sin 2\theta}{2}) \qquad \dots (ii)$

We know that the velocity of flow in an open channel,

 $Q = A.C.\sqrt{mi}$

We know that the velocity of flow in an open channel, $v = C\sqrt{mi}$

Problem: Find the maximum velocity of water in a circular channel of 500 mm radius, if the bed slope is 1 in 400. Take manning's constant as 50.

Solution:-

Given d= 500mm = 0.5m or r = 0.5/2 = 0.25m, i=1/400 and M= 50 Let 2θ = total angle (in radian) subtended by the water surface at the centre of the channel.

Now we know that for maximum velocity, the angle subtended by the water surface at the centre of the channel.

ANS

2 θ = 257°30' or θ = 128.75° = 128.75X $\overline{180}$ = 2.247rad ∴ Area of flow, $\mathbf{A} = r^2 (\theta - \frac{\sin 2 \theta}{2}) = 171 m^2$ And perimeter P = 2r θ = 1.124m ∴ hydraulic mean depth m= A/P = 0.171/1.124 = 0.152m

And velocity of water v= $MXm^{2/3}Xi^{\frac{1}{2}} = 0.71m/s$

Chapter-III

PUMPS

Centrifugal Pumps:-

The hydraulic machines which convert the mechanical energy to hydraulic energy are called pumps. The hydraulic energy is in the form of pressure energy. If the mechanical energy is converted, into pressure energy by means of centrifugal force acting on the fluid, the hydraulic machine is called centrifugal pump.

The centrifugal pump works on the principle of forced vortex flow which means that when a certain mass of liquid is rotated by an external torque, the rise in pressure head of the rotating liquid takes place. The rise in pressure head at any point of the rotating liquid is proportional to the square of tangential velocity of the liquid at that point (i.e., rise in pressure head $=\frac{v^2}{2g}or\frac{\omega^2 r^2}{2g}$). Thus at the outlet of the impeller, where radius is more, the rise in pressure head will be more & the liquid will be more & the liquid will be discharged at the outlet with a high pressure head. Due to this high pressure head, the liquid can be lifted

to a high level.

Main Parts Of A Centrifugal Pump:-

The followings are the main parts of a centrifugal pump:

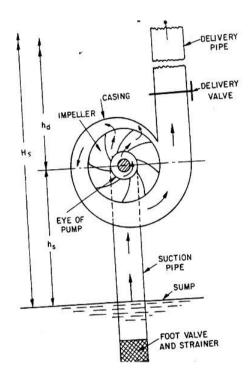
- 1. Impeller
- 2. Casing
- 3. Suction pipe with a foot valve & a strainer
- 4. Delivery Pipe

All the main parts of the centrifugal pump are shown in Fig 19.1

1. **Impeller**: The rotating part of a centrifugal pump is called 'impeller'. It consists of a series of backward curved vanes. The impeller is mounted on a shaft which is connected to the shaft of an electric motor.

2. **Casing:** The casing of a centrifugal pump is similar to the casing of a reaction turbine. It is an air-tight passage surrounding the impeller & is designed in such a way that the kinetic energy of the water discharged at the outlet of the impeller is converted into pressure energy before the water leaves the casing & enters the delivery pipe. The following three types of the casings are commonly adopted:

- a. Volute **casing** as shown in Fig.19.1
- b. Vortex casing as shown in Fig.19.2(a)
- c. Casing with guide blades as shown in Fig.19.2(b)
- a) Volute casing as shown in Fig.3.1the Volute casing, which is surrounding the impeller. It is of spiral type in which area of flow increases gradually. The increase in area of flow decrease velocity of flow. Decrease in velocity increases the pressure of water flowing through casing. it has been observed that in case of volute casing, the efficiency of pump increases.



Main parts of a centrifugal pump

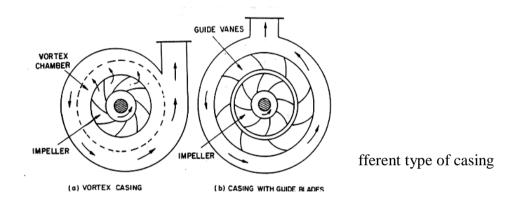
Fig. 3.1

b) **Vortex casing**. if a circular chamber is introduced between the casing and impeller as shown in fig.3.1,the casing is known as vortex casing .by introducing the circular chamber, loss of energy due to formation of eddies is reduced to a considerable extent. thus efficiency of pump is more than the efficiency when only volute casing is provided.

c) Casing with guide blades. This casing is shown in fig.3.1 in which the impeller is surrounded by a series of guide blades mounted on a ring which is known as diffuser. the guide vanes are designed in which a way that the water from the impeller enters the guide vanes without stock. Also the area of guide vanes increases, thus reducing the velocity of

flow through guide vanes and consequently increasing the pressure of water. the water from guide vanes then passes through the surrounding casing which is in most of cases concentric with the impeller as shown in fig.3.1.

3. **suction pipe with foot-valve and a strainer:** A pipe whose one end is connected to the inlet of pump and other end dips into water in a sump is known as suction pipe. A foot valve which is a non-return valve or one –way type valve is fitted at lower end of suction pipe. Foot valve opens only in upward direction. A strainer is also fitted at lower end of suction pipe.





4.**livery pipe:** a pipe whose one end is connected to outlet of pump and other end delivers water at a required height is known as delivery pipe.

Efficiencies of a centrifugal pump: Efficiencies of a centrifugal pump: In case of a centrifugal pump , the power is transmitted from the shaft of the electric motor to the shaft of the pump & then to the impeller. From the impeller, the power is given to the water. Thus power is decreasing from the shaft of the pump to the impeller & then to the water. The following are the important efficiencies of a centrifugal pump:

- *a*. Manometric efficiencies η_{man}
- b. Mechanical efficiencies η_m
- c. Overall efficiencies η_o
- a) **Manometric Efficiencies** η_{man} : The ratio of the manometric head to the head imparted by the impeller to the water is known as manometric efficiency. It is written as

 η_{max} = Manometric head/Head imparted by impeller to water

$$=\frac{H_m}{\frac{V_{w2}u_2}{g}}=\frac{gH_m}{V_{w2}u_2}$$
.....

The impeller at the impeller of the pump is more than the power given to the water at outlet of the pump. The ratio of the power given to water at outlet of the pump to the power available at the impeller, is known as manometric efficiency.

The power given to water at outlet of the pump= $\frac{WH_m}{1000}kW$

The power at the impeller = $\frac{Work \text{ done by impeller per second}}{1000} kW$

$$\frac{\frac{W}{g} \times \frac{V_{w2}u_2}{1000} kW}{\eta_{max}} = \frac{\frac{WH_m}{1000}}{\frac{W}{g} \times \frac{V_w2}{1000}} = \frac{V_{w2}gH_m}{V_{w2}}$$

b) Mechanical efficiencies:-

The power at the shaft of the centrifugal pump is more than the power available at the impeller of the pump. The ratio of the power available at the impeller to the power at the shaft of the centrifugal pump is known as mechanical efficiency. It is written as

 η_m = Power at the impeller/Power at the shaft

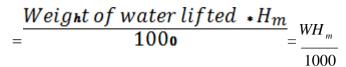
The power at the impeller in kW=work done by impeller per second/10000

$$= \frac{W}{g} \times \frac{V_{w2}u_2}{1000} \\ \eta_m = \frac{\frac{W}{g} \left(\frac{V_{w2}u_2}{1000} \right)}{S.P.} \dots$$

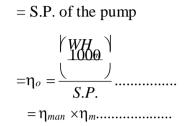
Where S.P.= Shaft Power

c) **Overall efficiencies** η_o

It is defined as the ratio of power output of the pump to the power input to the pump . The power output of the pump in kW



Power input to the pump =Power supplied by the electric motor



Problem 3.1: The internal & external diameters of the impeller of a centrifugal pump are 200mm & 400mm respectively. The pump is running at 1200 r.p.m. The vane angles of the impeller at inlet & outlet are $20^0 \& 30^0$ respectively. The water enters the impeller radially & velocity of flow is constant. Determine the velocity of flow per metre sec.

Solution: Internal Dia. Of impeller,=D₁=200mm=0.20m

External Dia. Of impeller ,=D₂=400mm=0.40m

Speed N=1200r.p.m

Vane angle at inlet , $\theta = 20^{\circ}$

Vane angle at outlet, $\phi = 30^{\circ}$

Water enter s radially means, $\alpha = 90^{\circ}$ and $V_{w1} = 0$

Velocity of flow , $=V_{f1} = V_{f2}$

Tangential velocity of impeller at inlet & outlet are,

$$u_1 = \frac{\Pi D_1 N}{60} = \frac{\Pi \times .20 \times 1200}{60} = 12.56 m / s$$
$$u_2 = \frac{\Pi D_2 N}{60} = \frac{\Pi \times .40 \times 1200}{60} = 25.13 m / s$$

From inlet velocity triangle,

50

$$\tan \phi = \frac{V_{f1}}{u_1} = \frac{V_{f2}}{12.56}$$
$$V_{f1} = 12.56 \tan \theta = 12.56 \times \tan 20 = 4.57 m / s$$
$$V_{f2} = V_{f1} = 4.57 m / s$$

Problem 3.2: A centrifugal pump delivers water against a net head of 14.5 metres & a design speed of 1000r.p.m. The values are back to an angle of 30^{0} with the periphery. The impeller diameter is 300mm & outlet width 50mm. Determine the discharge of the pump if manometric efficiency is 95%.

Solution: Net head, $H_{m=} 14.5m$

Speed, N =1000r.p.m

Vane angle at outlet, $\phi = 30^{\circ}$

Impeller diameter means the diameter of the impeller at outlet

Diameter, $D_2 = 300mm = 0.30m$

Outlet width, $B_2 = 50mm = 0.05m$

Manometric efficiency, $\eta_{man} = 95\% = 0.95$

Tangential velocity of impeller at outlet, $u_2 = \frac{\pi D_2 N}{60} = \frac{\pi \times .30 \times 1000}{60} = 15.70 m/s$

Now using equation

$$\eta_{\text{max}} = \frac{gH_m}{V_{w2}u_2}$$

$$0.95 = \frac{9.81 \times 14.5}{V_{w2} \times 15.70}$$

$$V_{w2} = \frac{0.95 \times 14.5}{0.95 \times 15.70} = 9.54 \text{m/s}$$



Refer to fig(3.3). From outlet velocity triangle, we have

$$\tan \phi = \frac{V_{f2}}{(u_2 - V_{w2})}$$

$$\tan 30^0 = \frac{V_{f2}}{(15.70 - 9.54)} = \frac{V_{f2}}{6.16}$$

$$V_{f2} = 6.16 \times \tan 30^0 = 3.556 m / s$$

Disch arg $e = Q = \pi \times D_2 \times B_2 \times V_{f2}$
$$= \pi \times 0.30 \times 0.05 \times 3.556 m^3 / s = 0.1675 m^3 / s$$

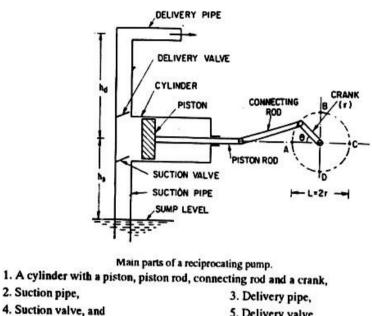
Reciprocating Pump:-

Introduction:-

We have defined the pumps as the hydraulic machines which convert the mechanical energy to hydraulic energy which is mainly in the form of pressure energy. If the mechanical energy is converted into hydraulic energy (or pressure energy) by sucking the liquid into a cylinder in which a piston is reciprocating (moving backwards and forwards), which exerts the thrust on the liquid & increases its hydraulic energy (pressure energy), the pump is known as reciprocating pump.

Main parts of a reciprocating pump:-

The following are the main parts of a reciprocating pump as shown in fig (3.4)



5. Delivery valve.

Fig. 3.4

Discharge through a Reciprocating Pump: Consider a single acting reciprocating pump as shown in fig ().

Let D= dia. Of the cylinder

A= C/s area of the piston or cylinder

$$=\frac{\pi}{4}D^2$$

r= Radius of crank

N=r.p.m of the crank

L=Length of the stroke=2*r

 h_s = height of the axis of the cylinder from water surface in sump

 h_d = Height of the delivery outlet above the cylinder axis (also called delivery head)

Volume of water delivered in one revolution or discharge of water in one revolution

= Area * Length of stroke = A*L

Ν

Number of revolution per second, = 60

Discharge of the pump per second , Q= Discharge in one direction \times No. of revolution per second

$$= A \times L^{\times} \frac{N}{60} = \frac{ALN}{60} \qquad \dots$$

Wt. of water delivered per second, $W = \rho g Q = \frac{\rho g A L N}{60}$

Work done by Reciprocating Pump : Work done by the reciprocating pump per sec. is given by the reaction as

Work done per second = Weight of water lifted per second \times Total height through which water is lifted

$$= W \times (h_s + h_d)$$

Where $(h_s + h_d)$ = Total height through which water is lifted

From equation () Weight, W is given by $W = \frac{\rho g A L N}{2}$ 60

Substituting the value of W in equation () we get

Work done per second =

 $\frac{\rho gALN}{60} \left(h_s + h_d \right) \dots$

Power required to drive the pump, in kW $\frac{\rho \times g \times ALN(h_s + h_d)}{60 \times 1000}$

 $=\frac{\rho gALN(h_s+h_d)}{60,000}kW$

 $\frac{Work \ done \ per \ second}{1000}$

=

.

P =

Classification of reciprocating pumps:

The reciprocating pumps may be classified as:

- 1. According to the water being in contact with one side or both sides of the piston, and
- 2. According to the number of cylinders provided

If the water is in contact with one side of the piston, the pump is known as single-acting. On the other hand,

If the water is in contact with both sides of the piston, the pump is called double –acting. Hence, classification according to the contact of water is:

- I. Single-acting pump
- II. Double –acting pump

According to the number of cylinder provided, the pumps are classified as:

- I. Single cylinder pump
- II. Double cylinder pump
- III. Triple cylinder pump

CHAPTER 10

DAMS

GRAVITY DAMS-EARTH DAMS

A **gravity dam** is a dam constructed from concrete or stone masonry and designed to hold back waterby primarily utilizing the weight of the material alone to resist the horizontal pressure of water pushing against it. Gravity dams are designed so that each section of the dam is stable, independent of any other dam section

FORCES ACTING ON GRAVITY DAM:

In the design of a dam, the first step is the determination of various forces which acts on the structure and study their nature. Depending upon the situation, the dam is subjected to the followingforces:

- 1. Water pressure
- 2. Earthquake forces
- 3. Silt pressure
- 4. Wave pressure
- Ice pressure
- 6. Self weight of the dam.

The forces are considered to act per unit length of the dam.

For perfect and most accurate design, the effect of all the forces should be investigated. Out of theseforces, most common and important forces are water pressure and self weight of the dam.

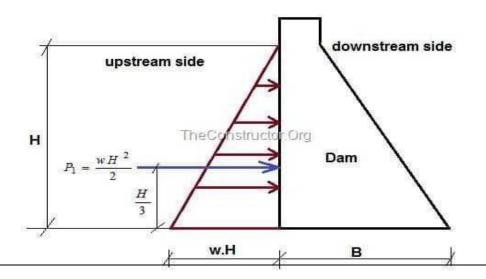
1. Water Pressure

Water pressure may be subdivided into the following two categories:

I) External water pressure:

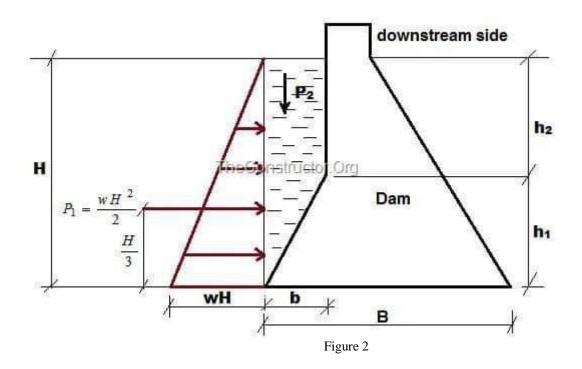
It is the pressure of water on the upstream face of the dam. In this, there are two cases:

(I) Upstream face of the dam is vertical and there is no water on the downstream side of the dam (figure 1).



The total pressure is in horizontal direction and acts on the upstream face at a height from the bottom. The pressure diagram is triangular and the total pressure is given by $\frac{P_{1}}{2} = \frac{wH^{2}}{2}$ Where w is the specific weight of water. Usually it is taken as unity.
H is the height upto which water is stored in m.

(ii) Upstream face with batter and there is no water on the downstream side (figure 2).



Here in addition to the horizontal water pressure P_1 as in the previous case, there is vertical pressure of the water. It is due to the water column resting on the upstream sloping side.

The vertical pressure P_2 acts on the length 'b' portion of the base. This vertical pressure is given by

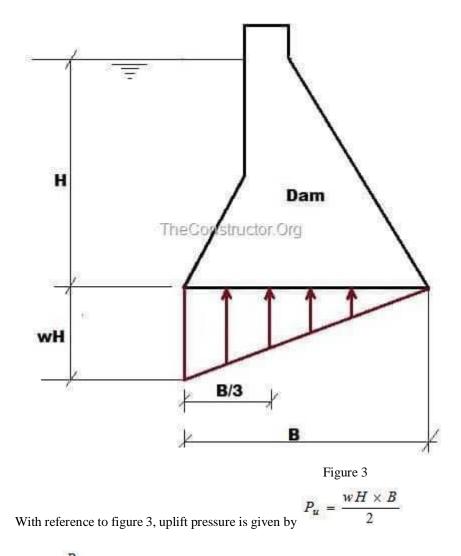
$$P_2 = (b \times h_2 \times w) + \left(\frac{1}{2}b \times h_1 \times w\right)$$

Pressure P_2 acts through the centre of gravity of the water column resting on the sloping upstreamface.

If there is water standing on the downstream side of the dam, pressure may be calculated similarly. The water pressure on the downstream face actually stabilizes the dam. Hence as an additional factor of safety, it may be neglected.

II) Water pressure below the base of the dam or Uplift pressure

When the water is stored on the upstream side of a dam there exists a head of water equal to the height upto which the water is stored. This water enters the pores and fissures of the foundation material under pressure. It also enters the joint between the dam and the foundation at the base and the pores of the dam itself. This water then seeps through and tries to emerge out on the downstream end. The seeping water creates hydraulic gradient between the upstream and downstream side of the dam. This hydraulic gradient causes vertical upward pressure. The upward pressure is known as uplift. Uplift reduces the effective weight of the structure and consequently the restoring force is reduced. It is essential to study the nature of uplift and also some methods will have to be devised to reduce the uplift pressure value.



Where P_u is the uplift pressure, B is the base width of the dam and H is the height upto which wateris stored.

This total uplift acts at $\overline{3}$ from the heel or upstream end of the dam.

Uplift is generally reduced by providing drainage pipes or holes in the dam section.

Self weight of the dam is the only largest force which stabilizes the structure. The total weight of the dam is supposed to act through the centre of gravity of the dam section in vertically downward direction. Naturally when specific weight of the material of construction is high, restoring force will be more. Construction material is so chosen that the density of the material is about 2.045 gram per cubic meter.

2. Earthquake Forces

The effect of earthquake is equivalent to acceleration to the foundation of the dam in the direction in which the wave is travelling at the moment. Earthquake wave may move in any direction and for design purposes, it is resolved into the vertical and horizontal directions. On an average, a value of

0.1 to 0.15g (where g = acceleration due to gravity) is generally sufficient for high dams in seismic zones. In extremely seismic regions and in conservative designs, even a value of 0.3g may sometimes by adopted.

Vertical acceleration reduces the unit weight of the dam material and that of water is to $(1 - k_v)$ times the original unit weight, where k_v the value of g accounted against earthquake forces, i.e. 0.1 is when 0.1g is accounted for earthquake forces. The horizontal acceleration acting towards the reservoir causes a momentary increase in water pressure and the foundation and dam accelerate towards the reservoir and the water resists the movement owing to its inertia. The extra pressure exerted by this process is known as hydrodynamic pressure.

3. Silt Pressure

If h is the height of silt deposited, then the forces exerted by this silt in addition to the external waterpressure, can be represented by Rankine formula

 $P_{\text{silt}} = \frac{1}{2} \gamma_s h^2 k_a \text{ acting at } \frac{h}{3}$ from the

base.Where,

 $1 - \sin \phi$

 $k_{\pi} = \text{coefficient of active earth pressure of silt} = \frac{1 + \sin \phi}{1 + \sin \phi}$ = angle of internal friction of soil, cohesion neglected. γ_{s} = submerged unit weight of silt material.

59

h = height of silt deposited.

4. Wave Pressure

Waves are generated on the surface of the reservoir by the blowing winds, which exert a pressure on the downstream side. Wave pressure depends upon wave height which is given by the equation

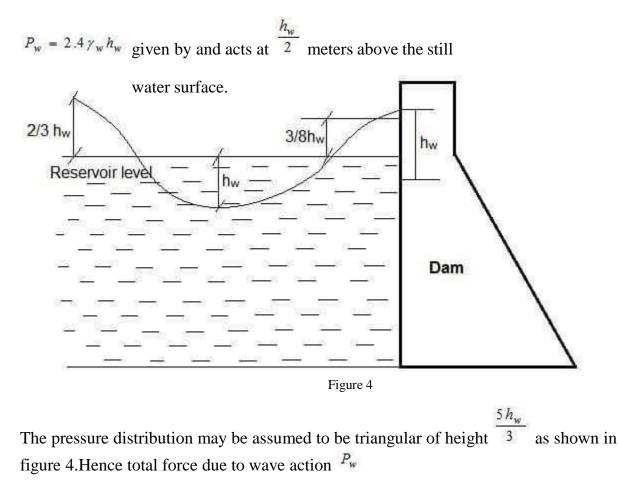
$$h_w = 0.032\sqrt{PV} + 0.763 - 0.271 \times (F)^{1/4}$$
 for F < 32 km, and
 $h_w = 0.032\sqrt{VF}$ for F > 32 km

Where h_w is the height of water from the top of crest to bottom of trough in

meters.V - wind velocity in km/hour

F – fetch or straight length of water expanse in km.

The maximum pressure intensity due to wave action may be



60

$$=\frac{1}{2} \times (2.4\gamma_w h_w) \times \frac{5}{3} h_w \text{ acting at } \frac{3}{8} h_w \text{ above the reservoir surface.}$$

5. Ice Pressure

The ice which may be formed on the water surface of the reservoir in cold countries may sometimes melt and expand. The dam face is subjected to the thrust and exerted by the expanding ice. This force acts linearly along the length of the dam and at the reservoir level. The magnitude of this force varies from 250 to 1500 kN/sq.m depending upon the temperature variations. On an average, a value of 500 kN/sq.m may be taken under ordinary circumstances.

6. Weight of dam

The weight of dam and its foundation is a major resisting force. In two dimensional analysis of dam

FAILURES OF GRAVITY DAM

Failure of gravity dam occurs due to overturning, sliding, tension and compression. A gravity dam is designed in such a way that it resists all external forces acting on the dam like water pressure, wind pressure, wave pressure, ice pressure, uplift pressure by its own self-weight. Gravity dams are constructed from masonry or concrete. However, concrete gravity dams are preferred these days and mostly constructed.

The advantage of gravity dam is that its structure is most durable and solid and requires very less maintenance.

Causes of failure of a Gravity Dam:

A gravity dam may fail in following modes:

- 1. Overturning of dam about the toe
- 2. Sliding shear failure of gravity dam
- 3. Compression by crushing of the gravity dam
- 4. Tension by development of tensile forces which results in the crack in gravity dam.

Overturning Failure of Gravity Dam:

The horizontal forces such as water pressure, wave pressure, silt pressure which act against the gravity dam causes overturning moments. To resist this, resisting moments are generated by the self-weight of the dam.

If the resultant of all the forces acting on a dam at any of its sections, passes through toe, the dam will rotate and overturn about the toe. This is called overturning failure of gravity dam. But, practically, such a condition does not arise and dam will fail much earlier by compression.

The ratio of the resisting moments about toe to the overturning moments about toe is called the factor of safety against overturning. Its value generally varies between 2 and 3.

Factor of safety against overturning is given by

FOS = sum of overturning moments/ sum of resisting moments

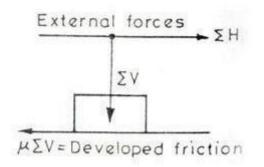


Fig:sum of external horizontal forces greater than vertical self-weight of dam (overacting, sliding occurs)

Sliding Failure of Gravity Dam:When the net horizontal forces acting on gravity dam at the base exceeds the frictional resistance (produced between body of the dam and foundation), The failure occurs is known as sliding failure of gravity dam.

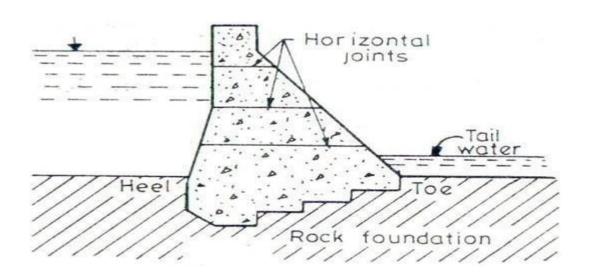
In low dams, the safety against sliding should be checked only for friction, but in high dams, for economical precise design, the shear strength of the joint is also considered

Factor of safety against sliding can be given based on Frictional resistance and shear strength of the dam

Factor of safety based on frictional resistance:

FOS against sliding = FOS = $\frac{\mu \sum V}{\sum H}$

 μ =co-efficient of friction between two surfaces $\sum V = \text{sum of vertical forces acting on dam}$ $\sum H = \text{sum of vertical forces acting on dam}$



Gravity Dam Failure due to Tension Cracks:Masonry and concrete are weak in tension. Thus masonry and concrete gravity dams are usually designed in such a way that no tension is developed anywhere. If these dams are subjected to tensile stresses, materials may develop tension cracks. Thus the dam loses contact with the bottom foundation due to this crack and becomes ineffective and fails. Hence, the effective width B of the dam base will be reduced. This will increase pmax at the toe. Hence, a tension crack by itself does not fail the structure, but it leads to the failure of the structure by producing excessive compressive stresses.

For high gravity dams, certain amount of tension is permitted under severest loading conditions in order to achieve economy in design. This is permitted because the worst condition of loads may occur only momentarily and may not occur frequently.

Gravity Dam Failure due to Compression:A gravity dam may fail by the failure of its material, i.e. the compressive stresses produced may exceed the allowable stresses, and the dam material may get crushed.

STABILITY ANALYSIS OF GRAVITY DAMS

General Selection of the method of analysis should be governed by the type and configuration of the structure being considered. The gravity method will generally be sufficient for the analysis of most structures, however, more sophisticated methods may be required for structures that are curved in plan, or structures with unusual configurations. 3-4.2 Gravity Method The gravity method assumes that the dam is a 2 dimensional rigid block. The foundation pressure distribution is assumed to be linear. It is usually prudent to perform gravity analysis before doing more rigorous studies. In most cases, if gravity analysis indicates that the dam is stable, no further analyses need be done.

Stability Analysis Assumptions:

- 1. The dam is considered to be composed of a number of Cantilevers, each of which is 1 m thick and each of which acts independently of the other.
- 2. No load is transferred to the abutments by beam action
- 3. The foundation and the dam behave as a single unit, the joints being perfect.
- 4. The material in the foundation and the body of the dam are isotropic and homogeneous.
- 5. The stresses developed in the foundation and the body of the dam is isotropic and homogeneous.
- 6. No movements of dams are caused by the Transfers of loads.

Stability Analysis Procedure

Two dimensional analysis can be carried out analytically or graphically

Analytical Method

- 1. Consider unit length of the dam
- 2. Work out the magnitude and direction of all the vertical forces acting on the dam and their algebraic sum i.e. $\sum V$
- 3. Similarly, work out all the horizontal forces and their algebraic sum, i.e., $\sum H$
- 4. Determine the level arm of all these forces about the toe
- 5. Determine the moments of all these forces about the toe and find out the algebraic sum of all those moments i.e., $\sum M$

Graphical method

In the graphical method, the entire dam section is divided into number of horizontal sections at somesuitable interval. Particularly at the place where the slope changes.

- 1. For each section, the sum of the vertical forces $\sum V$ and the sum of all the horizontal forces $\sum H$ acting above that particular section, are worked out and the resultant is drawn, graphically
- 2. This is done for each section and a line joining all the points where the individual resultants cut the individual sections, is drawn.
- 3. This line represents the resultant force and should lie within the middle third, for no tensionto develop.
- 4. The procedure should be repeated for reservoir full as well reservoir empty case.

Profile of A Dam from Practical Considerations

• The elementary profile of a gravity dam, (i.e., triangle with maximum water surface at apex) is only a theoretical profile. Certain changes will have to be made in this profile in order to cater to the practical needs.

These needs are,

(i) Providing a straight top width for road construction over the top of the dam

(ii) Providing a free-board above the top water surface, so that water may spill over the top of the dam due to wave action, etc.

The addition of these two provisions, will cause the resultant force to shift towards the heel. The resultant force, when the reservoir is empty, was earlier passing through the inner middle thirdpoint. This will, therefore, shift more towards the heel, crossing the inner middle third point and consequently, tension will be developed at the toe. In order to avoid the development of thistension, some masonry will have to be added to the upstream side., which shows the typical section along with the possible dimensions that can be adopted for a low gravity dam section. It should however, be checked for stability analysis.

Galleries in Gravity Dams

Galleries are the horizontal or sloping openings or passages left in the body of the dam. • They may run longitudinally (i.e. parallel to dam axis) or traversely (i.e. normal to the dam axis) and are provided at various elevations. All the galleries are interconnected by steeply sloping passages or by vertical shafts fitted with stairs or mechanical lifts.

Function and types of galleries in Dams

(i) Foundation Gallery

A gallery provided in a dam may serve one particular purpose or more than one purpose. For example, a gallery provided near the rock foundation, serves to drain off the water which percolates through the foundations. This gallery is called a foundation gallery or a drainage gallery.

- 1. It runs longitudinally and is quite near to the upstream face of the dam. Drain holes are drilled from the floors of this gallery after the foundation grouting has been completed. Seepages is collected through these drain holes.
- 2. Besides draining off seepage water, it may be helpful for drilling and grouting of the foundations, when this can not be done from the surface of the dam.

(ii)Inspection Galleries

The water which seeps through the body of the dam is collected by means of a system of galleries provided at various elevations and interconnected by vertical shafts, etc. All these galleries, besides draining off seepage water, serves inspection purpose. They provide access to the interior of the dam and are, therefore, called inspection purposes. They generally serve other purposes along with this purpose.

- 1. They intercept and drain off the water seeping through the dam body
- 2. They provide access to dam interior for observing and controlling the behavior of the dam.
- 3. They provide enough space for carrying pipes, etc. during artificial cooling of concrete
- 4. They provide access to all the outlets and spillway gates, valves, etc. by housing their electrical and mechanical controls. All these gates, valves, etc, can hence be easily controlled by men, from inside the dam itself.

5. They provide space for drilling and grouting of the foundations, then it cannot be done from the surface of the dam.

EARTH DAMS

An **embankment dam** is a large artificial dam. It is typically created by the placementand compaction of a complex semi-plastic mound of various compositions of soil, sand, clay, or rock. It has a semi-pervious waterproof natural covering for its surface and a dense, impervious core. This makes such a dam impervious to surface or seepage erosion.^[1] Such a dam is composed of fragmented independent material particles. The friction and interaction of particles binds the particles togethe<u>r</u> into a stable mass rather than by the use of a cementing substance.

Embankment dams come in two types: the **earth-filled dam** (also called an earthen dam or terrain dam) made of compacted earth, and the **rock-filled dam**. A cross-section of an embankment dam shows a shape like a bank, or hill. Most have a central section or core composed of an impermeable material to stop water from seeping through the dam. The core can be of clay, concrete, or asphalt concrete. This dam type is a good choice for sites with wide valleys. They can be built on hard rock or softer soils. For a rock-fill dam, rock-fill is blasted using explosives to break the rock. Additionally, the rock pieces may need to be crushed into smaller grades to get the right range of size for use in an embankment dam

The building of a dam and the filling of the reservoir behind it places a new weight on the floor and sides of a valley. The stress of the water increases linearly with its depth. Water also pushes against the upstream face of the dam, a nonrigid structure that under stress behaves semiplastically, and causes greater need for adjustment (flexibility) near the base of the dam than at shallower water levels. Thus the stress level of the dam must be calculated in advance of building to ensure that its break level threshold is not exceeded.

Overtopping or overflow of an embankment dam beyond its spillway capacity will cause its eventual failure. The erosion of the dam's material by overtopping runoff will remove masses of material whose weight holds the dam in place and against the hydraulic forces acting to move the dam. Even a small sustained overtopping flow can remove thousands of tons of overburden soil from the mass of the dam within hours. The removal of this mass unbalances the forces that stabilize the dam against its reservoir as the mass of water still impounded behind the dam presses against the lightened mass of the embankment, made lighter by surface erosion. As the mass of the dam erodes, the force exerted by the reservoir begins to move the entire structure. The embankment, having almost no elastic strength, would begin to break into separate pieces, allowing the impounded reservoir water to flow between them, eroding and removing even more material as it passes through. In the final stages of failure the remaining pieces of the embankment would offer almost no resistance to the flow of the water and continue to fracture into smaller and smaller sections of earth or rock until these would disintegrates into a thick mud soup of earth, rocks and water.

Therefore, safety requirements for the spillway are high, and require it to be capable of containing a maximum flood stage. It is common for its specifications to be written such that it can contain a five hundred year flood. Recently a number of embankment dam overtopping protection systems have

been developed. These techniques include the concrete overtopping protection systems, timber cribs, sheet-piles, riprap and gabions, reinforced earth, minimum energy loss weirs, embankment overflow stepped spillways and the precast concrete block protection systems.

The two principal types of embankment dams are earth and rock-fill dams, depending on the predominant fill material used. Some generalized sections of earth dams showing typical zoning for different types and quantities of fill materials When practically only one impervious material is available and the height of the dam is relatively low, a homogeneous dam with internal drain. The inclined drain serves to prevent the downstream slope from becoming saturated and susceptible to piping and/or slope failure and to intercept and prevent piping through any horizontal cracks traversing the width of the embankment.

Earth Dam with impervious cores, are constructed when local borrow materials do not provide adequate quantities of impervious material. A vertical core located near the center of the dam is preferred over an inclined upstream core because the former provides higher contact pressure between the core and foundation to prevent leakage, greater stability under earthquake loading, andbetter access for remedial seepage control. An inclined upstream core allows the downstream portion of the embankment to be placed first and the core later and reduces the possibility of hydraulic fracturing. However, for high dams in steep-walled canyons the overriding consideration is the abutment topography. The objective is to fit the core to the topography in such a way to avoid divergence, abrupt topographic discontinuities, and serious geologic defects. For <u>dams</u> on pervious foundations, seepage control is necessary to prevent excessive uplift pressures and piping throughthe foundation.

The methods for control of under seepage in dam foundations are horizontal drains, cutoffs (compacted backfill trenches, slurry walls, and concrete walls), upstream impervious blankets, downstream seepage berms, toe drains, and relief wells. A rock-fill dam with steep slopes requires better foundation conditions than an earth dam, and a concrete dam (or roller-compacted concrete dam) requires better foundation conditions than a rock-fill dam.

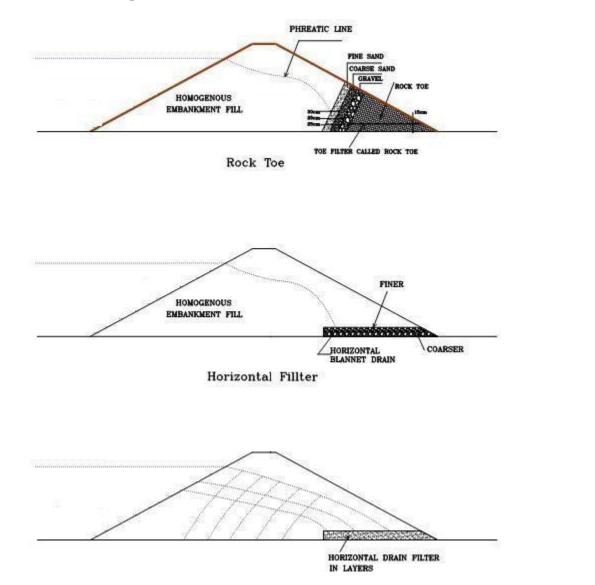
An earth dam is composed of suitable soils obtained from borrow areas or required excavation and compacted in layers by mechanical means. Following preparation of a foundation, earth from borrows areas and from required excavations is transported to the site, dumped, and spread in layers of required depth. The soil layers are then compacted by tamping rollers; sheep foot rollers, heavy pneumatic-tired rollers, vibratory rollers, tractors, or earth-hauling equipment. One advantage of an earth dam is that it can be adapted to a weak foundation, provided proper consideration is given to thorough foundation exploration, testing, and design.

Phreatic Line and Horizontal Drain In Earth fill Dams

Earth dams are generally built of locally available materials in their natural state with a minimum of processing. Homogeneous earth dams are built whenever only one type of material is economically available.

The material must be sufficiently impervious to provide an adequate water barrier and slopes must be relatively flat to make it safe against piping and sloughing.

The general design procedure is to make a first estimate on the basis of experience with similar dams and then to modify the estimate as required after conducting a stability analysis except where there is a surplus of material.



The upstream slopes of most of the earth dams in actual practice usually vary from 2.0 (horizontal):1 (vertical) to 4:1 and the downstream slopes are generally between 2:1 and 3:1 (USBR 2003). Free board depends on the height and action of waves. USBR (2003) recommends normal free-board about 1.5 to 3 m depending on the fetch. The width of the dam crest is determined by considering the nature of embankment materials, height and importance of structure, possible roadways requirements, and practicability of construction. A majority of dams have the crest widths varying between 5 and 12 m.

About 30% of dams had failed due to the seepage failure, viz piping and sloughing. Recent comprehensive reviews by Foster et al. (2000a,b) and Fell et al. (2003) show that internal erosion and piping are the main causes of failure and accidents affecting embankment dams; and the proportion of their failures by piping increased from 43% before 1950 to 54% after 1950. The sloughing of the downstream face of a homogeneous earth dam occurs under the steady-state seepage condition due to the softening and weakening of the soil mass when the top flow line or phreatic line intersects it. Regardless of flatness of the downstream slope and impermeability of soil, the phreatic line intersects the downstream face to a height of roughly one-third the depth of water . It is usual practice to use a modified homogeneous section in which an internal drainage system in the form of a horizontal blanket drain or a rock toe or a combination of the two is provided. The drainage system keeps the phreatic line well within the body of the dam. Horizontal filtered drainage blankets are widely used for dams of moderate height.USBR constructed the 50 m high Vega dam, which is one of the highest with a homogenous section and a horizontal downstream drain.

The minimum length of the horizontal blanket drain required to keep the phreatic line within the body of the dam by a specified depth and also equations for maximum downstream slope cover and minimum and maximum effective lengths of the downstream filtered drainage system.

The position of the phreatic line influences the stability of the earth dam because of potential piping due to excessive exit gradient and sloughing due to the softening and weakening of the soil mass as if it touches the downstream slope or intersects it. When the dam embankment is homogeneous or when the downstream zone is of questionable permeability, a horizontal drainage blanket is provided to keep the phreatic line well within the dam body, to allow adequate embankment and foundation drainage, and to eliminate piping from the foundation and the embankment.

As the dams are made of fine-grained soil, saturation may occur due to the capillary rise above the phreatic surface so it is necessary to account for capillary rise while calculating the minimum length of the downstream filtered drainage. Though the suction head in the soil matrix above the phreatic surface within the dam body due to capillary rise generally improves the stability of the downstream slope, once the capillary fringe intersects the downstream slope the pressure changes from negative (suction) to atmospheric and the downstream face may become a seepage face leading to its failure. Hence the phreatic line should not intersect the downstream slope and it should be a distance greater than capillary rise below the sloping face so that the chances of the sloughing or piping may be nullified.

Stability and Failure of Earth Filled Dams

Failure of earth dams may be:

- 1. Hydraulic Failure
- 2. Seepage Failure
- 3. Structural Failure

1. Hydraulic Failure:

- 1. Overtopping of dams
- 2. Erosion of the Upstream Surface
- 3. Erosion of the Downstream Surface
- 4. Erosion of the Downstream toe

i. Overtopping of dams:

This type of dam is made up of only one type of material. Usually porous materials is used. These dams are easy and cheap to construct but cannot be used to make multipurpose large dams. For large multipurpose dams zoned type method is used. Over topping failures result from the erosive action of water on the embankment. Erosion is due to un-controlled flow of water over, around, and adjacent to the dam. Earth embankments are not designed to be over-topped and therefore are particularly susceptible to erosion. Once erosion has begun during over-topping, it is almost impossible to stop. A well vegetated earth embankment may withstand limited over topping if its crest is level and water flows over the crest and down the face as an evenly distributed sheet without becoming concentrated. The owner should closely monitor the reservoir pool level during severe storms.

ii. Erosion of the Upstream Surface:

Here zones of different materials are made.

Shell is used to give support and stability to the structure of dam. It is made of coarse materials and is pervious in nature.

Core is used to make the dam water tight and to reduce the seepage. Fine material is used here.Used in large dams.

iii. Erosion of the Downstream Surface:

Due to rainfall, snow and winds the downstream surface of the dam also erodes. By providing a section of coarse materials here, this erosion can be reduced or prevented.

2. Seepage Failure:

All earth dams have seepage resulting from water permeating slowly through the dam and its foundation. Seepage must be controlled in both velocity and quantity. If uncontrolled, it can progressively erode soil from the embankment or its foundation, resulting in rapid failure of the dam. Erosion of the soil begins at the downstream side of the embankment, either in the dam proper or the foundation, progressively works toward the reservoir, and eventually develops a direct connection to the reservoir. This phenomenon is known as "piping." Piping action can be recognized by an increased seepage flow rate, the discharge of muddy or discolored water, sinkholes on or near the embankment, or a whirlpool in the reservoir. Once a whirlpool (eddy) is observed on the reservoir surface, complete failure of the dam will probably follow in a matter of minutes. As with over topping, fully developed piping is virtually impossible to control and will likely cause failure. Seepage can cause slope failure by creating high pressures in the soil pores or by saturating the slope. The pressure of seepage within an embankment is difficult to determine without proper

instrumentation. A slope which becomes saturated and develops slides may be showing signs of excessive seepage pressure.

Seepage failure of the dams is of the following types

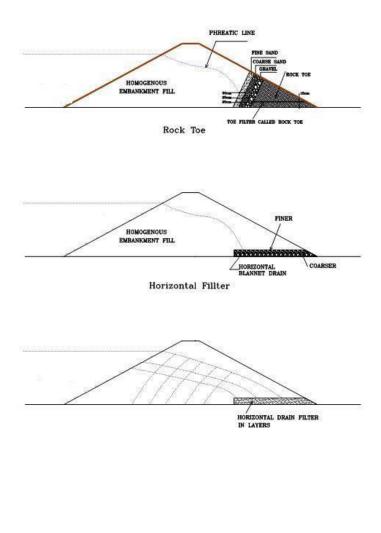
- 1. Piping through the dam
- 2. Piping through the foundation
- 3. Conduit Leakage
- 1. **Piping thorugh the dam:** There are two kinds of forces acting on the downstream face of the dam:
 - 1. Weight of the material
 - 2. Seepage Force

If the seepage force exceeds the weight of the material the water washes away the soil from theplate and creates a hole in the ground. This hole deepens as more and more mateial is taken away from it and extends longitudinally, making a pipe hole called "Piping in the dam".

3. Structural Failure:

Structural failures can occur in either the embankment or the appurtenances. Structural failure of a spillway, lake drain, or other appurtenance may lead to failure of the embankment.

Cracking, settlement, and slides are the more common signs of structural failure of embankments. cracks in either Large an appurtenance or the embankment, major settlement, and major slides will require emergency measures to ensure safety, especially if these problemsoccur suddenly. If this type of situation occurs, the lake level should be lowered, the appropriate state and local authorities notified. and professional advice sought. If the observer is uncertain as to the seriousness of the problem, the Division of Water should be contacted immediately. The three types of failure previously described



are often interrelated in a complex manner. For example, uncontrolled seepage may weaken the soil and lead to a structural failure. A structural failure may shorten the seepage path and lead to a piping failure. Surface erosion may result in structural failure.

- 1. Failure of downstream face during steady seepage conditions
- 2. Failure of upstream face during sudden draw down
- 3. Failure due to sliding of foundation
- 4. damage due to burrowing animals
- 5. Failure of dam due to earthquake
- Usually upper part of the dam is dry and the lower is saturated with water which gives rise to pore water pressure within the voids. Dam body is saturated - All pores / voids are filled with water, pore water pressure is induced. Effective pressure reduces and shear strength of soil decreases
- 2. When water is suddenly withdrawn or in other words if the level of water in the reservoir reduces suddenly, the soil on the upstream face of the dam body may be highly saturated andhas pore water pressure that tries to destabilise the dam and if this force is high enough, it can fail the dam.
- 3. If the shear strength of the soil on which the foundation is built is weak though the foundation itself may be strong but due to weakness of the soil foundation may slide on the sides and in some cases the foundation itself may be not able to resist the shear force that may have increased from normal due to any reason.
- 4. Burrowing animals Small animals living in the holes and pits may have dug theri holes anywhere in te dam body which may widen with the passage of time and can be dangerous.
- 5. Earthquake

Minor defects such as cracks in the embankment may be the first visual sign of a major problem which could lead to failure of the structure. The seriousness of all deficiencies should be evaluated by someone experienced in dam design and construction. A qualified professional engineer can recommend appropriate permanent remedial measures.